

Package ‘flowCyBar’

January 23, 2026

Encoding UTF-8

Type Package

Title Analyze flow cytometric data using gate information

Version 1.47.0

Date 2015-03-05

Author Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Susanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <ingo.fetzer@stockholmresilience.su.se>, Susann Müller <susann.mueller@ufz.de>

Maintainer Joachim Schumann <joachim.schumann@ufz.de>

Description A package to analyze flow cytometric data using gate information to follow population/community dynamics

License GPL-2

URL <http://www.ufz.de/index.php?de=16773>

biocViews ImmunoOncology, CellBasedAssays, Clustering, FlowCytometry, Software, Visualization

Depends R (>= 3.0.0)

Imports gplots, vegan, methods

Collate AllGenerics.R normalize.R cybar_plot.R nmads.R correlation.R

git_url <https://git.bioconductor.org/packages/flowCyBar>

git_branch devel

git_last_commit 8c80d76

git_last_commit_date 2025-10-29

Repository Bioconductor 3.23

Date/Publication 2026-01-23

Contents

flowCyBar-package	2
Abiotic_data_sample	3
Cell_number_sample	3
correlation	3
Corr_data_sample	5
cybar_plot	6
nm ds	9
normalize	11
Index	14

flowCyBar-package	Analyze flow cytometric data
-------------------	------------------------------

Description

A package to analyze flow cytometric data

Details

Package: CyBar
Type: Package
Version: 1.0
Date: 2014-02-14
License: GPL-2

Cell_number Cell_number_nmds Cell_number_sample Corr_data Corr_data_sample correlation
flowCyBar cybar_plot nm ds normalize Normalized_first Normalized_mean Normalized_nmds

Author(s)

Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Su-
sanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <info.fetzer@stockholmresilience.su.se>,
Susann Müller <susann.mueller@ufz.de>

Abiotic_data_sample	<i>Dataset with abiotic data and sample names</i>
---------------------	---

Description

Example dataset containing normalized cell numbers and abiotic parameters used for the NMDS plot.

Usage

```
data(Abiotic_data_sample)
```

Format

Data frame with 10 observations of 44 variables.

Cell_number_sample	<i>Dataset with relative measured cell numbers and sample names</i>
--------------------	---

Description

Example dataset of relative measured cell numbers with sample names.

Usage

```
data(Cell_number_sample)
```

Format

Data frame with 10 observations of 31 variables.

correlation	<i>Visualize the correlation</i>
-------------	----------------------------------

Description

A function to visualize the correlation of the relative or percental cell numbers and the abiotic parameters.

Usage

```
## S4 method for signature 'data.frame'
correlation(x, cortype="spearman", exact=FALSE, colkey=bluered(21), Rowv=TRUE, Colv=TRUE, symm=TRUE, distf

## S4 method for signature 'matrix'
correlation(x, cortype="spearman", exact=FALSE, colkey=bluered(21), Rowv=TRUE, Colv=TRUE, symm=TRUE, distf
```

Arguments

<code>x</code>	Data frame or matrix of correlation values. Use one row per sample and one column per gate/abiotic parameter. Use the first column for the first gate/abiotic parameter. The names of the gates and abiotic parameters may not contain any whitespace. If the values contain commas they must be expressed as ".". Missing values or NA's are allowed but should be expressed as "NA" or empty entries within the table.
<code>cortype</code>	Character string indicating which correlation coefficient is used. Choose between <i>"spearman"</i> (default), <i>"kendall"</i> and <i>"pearson"</i> . See Details for more information.
<code>exact</code>	logical (default=FALSE). Do not compute exact p-values. Used for Kendall's tau and Spearman's rho. Can be changed to TRUE if R can compute exact p-values without ties. Computing exact p-values depends on the dataset. For more details type <i>"?cor.test"</i> into R command line.
<code>colkey</code>	Indicating the color key/palette used for visualization (default= <i>bluered(21)</i>). See Details for more information.
<code>Rowv</code>	logical (default=TRUE). The row dendrogram will be arranged according to similarity. FALSE will arrange the dendrogram according to the sequence of data e.g. according to sampling.
<code>Colv</code>	logical (default=TRUE). Determines how the column dendrogram should be re-ordered. Has the same options as the Rowv argument above.
<code>symm</code>	logical (default=TRUE). Indicates if x should be treated symmetrically. Can only be TRUE if x is a square matrix.
<code>distfun</code>	Function used for the computation of the distance (dissimilarity) between both rows and columns (default=function(c) as.dist(1 - c)).
<code>dendrogram</code>	Character string indicating whether dendrograms should be displayed (default= <i>"both"</i>). Can be changed to <i>"row"</i> , <i>"column"</i> or <i>"none"</i> . Rowv/Colv has to be set TRUE to show a dendrogram for the rows/columns.
<code>main</code>	Character string used as title of the correlation heatmap (default="")
<code>verbose</code>	logical (default=FALSE). Change to TRUE to print estimates and additional information to the heatmap.
<code>...</code>	Additional heatmap parameters. For more details type <i>"?heatmap.2"</i> into R command line.

Details

Visualize the correlations between the cell number variations and abiotic parameters as a heatmap using the `heatmap.2` function of the package "gplots" (see reference Warnes et al. 2013). Spearman's rank-order correlation coefficient (r_S) is used for this purpose, by default (see reference Koch et al. 2013, Box 1 for more details). This value varies between -1 and 1. The stronger the correlation, the closer the value of the coefficient to 1 (for positive correlations) or -1 (for negative correlations). Kendall's tau rank correlation coefficient also assigns the values to ranks but considers the difference between the probability that any two points will agree on the relative ranks compared to the probability that they will disagree. Pearson's product-moment correlation coefficient uses the true values and can be chosen to depict linear relationships. You can choose the color key/palette

and the gradations for visualization. By choosing the default color key positive correlations will be shown in shades of red, negative correlations will be shown in shades of blue and neutral correlations will be shown in white. Other possibilities are e.g. `topo.colors(16)`, `cm.colors(15)` or `heat.colors(11)`. The space within the brackets defines the gradations of the color key. For more details type `"??Palettes"` into R command line. It is also possible to define an own color palette. For more details on that type `"?colorRampPalette"` into R command line.

Author(s)

Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Susanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <info.fetzer@stockholmresilience.su.se>, Susann Müller <susann.mueller@ufz.de>

References

Koch, Christin and Günther, Susanne and Desta, Adey Feleke and Hübschmann, Thomas and Müller, Susann (2013). Cytometric fingerprinting for analysing microbial intra-community structure variation and identifying sub-community function. *Nature Protocols*, 8(1):190-202,

Gregory R. Warnes, Ben Bolker, Lodewijk Bonebakker, Robert Gentleman, Wolfgang Huber Andy Liaw, Thomas Lumley, Martin Maechler, Arni Magnusson, Steffen Moeller, Marc Schwartz and Bill Venables (2013). *gplots: Various R programming tools for plotting data*. R package version 2.12.1. <http://CRAN.R-project.org/package=gplots>

Examples

```
require(gplots)

## Show the correlation saved in dataset Corr_data_sample
## Use default parameters

data(Corr_data_sample)
correlation(Corr_data_sample[, -1])

## Change the title to "Correlation heatmap"
## Use palette heat.colors(11) as color key

data(Corr_data)
correlation(Corr_data_sample[, -1], colkey=heat.colors(11), main="Correlation heatmap")
```

Corr_data_sample

Dataset with correlation data and sample names

Description

Example dataset containing relative measured cell numbers and abiotic parameters for correlation analysis.

Usage

```
data(Corr_data_sample)
```

Format

Data frame with 10 observations of 44 variables.

cybar_plot	<i>Barcode of the normalized cell numbers and boxplot of relative or percental cell numbers</i>
------------	---

Description

Show a barcode of the variation of normalized cell numbers (CyBar plot) and a boxplot of the relative or percental cell numbers.

Usage

```
## S4 method for signature 'data.frame,data.frame'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",dendrogram="col",from=0,to=2,na.col=
order="original",boxmain="",verbose=FALSE,...)

## S4 method for signature 'matrix,matrix'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",
dendrogram="col",from=0,to=2,na.color="black",barmain="",labels="hor",
order="original",boxmain="",verbose=FALSE,...)

## S4 method for signature 'data.frame,matrix'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",dendrogram="col",from=0,to=2,na.col=
order="original",boxmain="",verbose=FALSE,...)

## S4 method for signature 'matrix,data.frame'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",dendrogram="col",from=0,to=2,na.col=
order="original",boxmain="",verbose=FALSE,...)

## S4 method for signature 'data.frame,missing'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",
dendrogram="col",from=0,to=2,na.color="black",barmain="",verbose=FALSE,...)

## S4 method for signature 'matrix,missing'
cybar_plot(x,y,Rowv=FALSE,grad=21,trace="none",tracecol="black",
dendrogram="col",from=0,to=2,na.color="black",barmain="",verbose=FALSE,...)

## S4 method for signature 'missing,data.frame'
cybar_plot(x,y,labels="hor",boxmain="",verbose=FALSE,...)

## S4 method for signature 'missing,matrix'
cybar_plot(x,y,labels="hor",boxmain="",verbose=FALSE,...)
```

Arguments

x	Data frame or matrix of normalized cell numbers. Use one row per sample and one column per gate. Use the first column for the first gate. The names of the gates may not contain any whitespace. If the values contain commas they must be expressed as ".". Missing values or NA's are allowed but should be expressed as "NA" or empty entries within the table.
y	Data frame or matrix of relative or percental cell numbers. Same requirements as described for x.
Rowv	Keeps sequence of data in the barcode e.g. according to sampling (default=FALSE). If TRUE it will be arranged according to similarity.
grad	Gradations of the color key used in the barcode (default=21).
trace	Display trace lines in the barcode (default="none"). For displaying trace lines choose between "column", "row" or "both".
tracecol	Color of traces in the barcode if trace is active (default="black").
dendrogram	Character string indicating whether dendrograms should be displayed in the barcode (default="column"). Can be changed to "row", "both" or "none". If you want to display a dendrogram for the rows and columns change to "both" and Rowv to TRUE.
from	Beginning of the data range of the normalized cell numbers (default=0).
to	End of the data range of the normalized cell numbers (default=2).
na.color	Color used for missing values or NA (default="black").
barmain	Character string used as title of the barcode (default="").
labels	Character string indicating whether horizontal ("hor") data labels (default) or vertical ("vert") data labels should be plotted in the boxplot.
order	Character string indicating the order of the gates in the boxplot (default="original"). The boxes are ordered respective to the original order of the gates. Choose "sim" if the boxes should be ordered respective to the similarity calculated in the heatmap function. This can only be done if x is given and the barcode is created.
boxmain	Character string used as title of the boxplot (default="").
verbose	logical (default=FALSE). Change to TRUE to print additional information to the barcode and/or the boxplot.
...	Additional plotting parameters used for the heatmap and the boxplot. For more details type "?heatmap.2" or "?boxplot" into R command line.

Details

This function generates a barcode of the normalized cell numbers for all measurements using the heatmap.2 function of the package "gplots" (see reference Warnes et al. 2013). The barcode displays the variation for each gate using a color key with 21 gradations. Very low values are shown in blue, intermediate values are shown in white and high values are shown in deep red. Missing values or NA's are shown in black. In addition a dendrogram to reveal clusters and a histogram of the values are shown. The distribution of the relative or percental cell numbers per gate is visualized as a vertical

boxplot. One box consists of the median, the upper and lower quartil (top and bottom of the box) containing 50% of the data, whiskers showing the minimum (within 1.5-fold of the interquartile range of the lower quartile) and the maximum (within 1.5-fold of the interquartile range of the upper quartile) of the data and outliers. Choose between horizontal ("hor") and vertical ("vert") data labels that represent the gates. See reference Koch et al. 2013 for more details.

Author(s)

Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Susanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <info.fetzer@stockholmresilience.su.se>, Susann Müller <susann.mueller@ufz.de>

References

Koch, Christin and Günther, Susanne and Desta, Adey Feleke and Hübschmann, Thomas and Müller, Susann (2013). *Cytometric fingerprinting for analysing microbial intra-community structure variation and identifying sub-community function*. *Nature Protocols*, 8(1):190-202,

Gregory R. Warnes, Ben Bolker, Lodewijk Bonebakker, Robert Gentleman, Wolfgang Huber Andy Liaw, Thomas Lumley, Martin Maechler, Arni Magnusson, Steffen Moeller, Marc Schwartz and Bill Venables (2013). *gplots: Various R programming tools for plotting data*. R package version 2.12.1. <http://CRAN.R-project.org/package=gplots>

Examples

```
require(gplots)

## Show a barcode of the normalized cell numbers
## and a boxplot with horizontal data labels of the percental cell numbers
## saved in dataset Cell_number_sample
## The boxes are ordered according to the original order

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
cybar_plot(Normalized_mean,Cell_number_sample[,-1])

## Barcode and boxplot are titled according to the dataset names, respectively
## The orientation of the data labels is vertical

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
cybar_plot(Normalized_mean,Cell_number_sample[,-1],
barmain="Barcode of normalized cell numbers",labels="vert",boxmain="Boxplot of cell numbers")

## Show a barcode of the normalized cell numbers using method "first"
## The end of the data range of the normalized cell numbers is set to 3.5
## The boxes are ordered according to the similarity calculated in the barcode

data(Cell_number_sample)
Normalized_first<-normalize(Cell_number_sample[,-1],method="first",digits=2)
```



```
Normalized_first<-data.frame(data.matrix(Normalized_first))
cybar_plot(Normalized_first,Cell_number_sample[,-1],to=3.5,
barmain="Barcode of normalized cell numbers",labels="vert",order="sim",boxmain="Boxplot of cell numbers")
```

nmds

NMDS plot of cell numbers

Description

NMDS plot of the relative/percental or normalized cell numbers.

Usage

```
## S4 method for signature 'data.frame'
nmds(x,distance="bray",autotransform=FALSE,zerodist="add",group,main="",type="p",
cex=0.6,pos=4,shrink=TRUE,legend_pos="topleft",pch=1,col="black",abiotic,p.max=0.05,col_abiotic="ma

## S4 method for signature 'matrix'
nmds(x,distance="bray",autotransform=FALSE,zerodist="add",group,main="",type="p",
cex=0.6,pos=4,shrink=TRUE,legend_pos="topleft",pch=1,col="black",abiotic,p.max=0.05,col_abiotic="ma
```

Arguments

x	Data frame or matrix of relative/percental cell numbers or normalized cell numbers. Use one row per sample and one column per gate. Use the first column for the first gate. The names of the gates may not contain any whitespace. If the values contain commas they must be expressed as ".". Missing values or NA's are not allowed.
distance	Dissimilarity index used in vegdist (default=" <i>bray</i> "). For more details type "?metaMDS" into R command line.
autotransform	logical (default=FALSE). Determine the use of simple heuristics for a possible data transformation of typical community data. For more details type "?metaMDS" into R command line.
zerodist	Handling of zero dissimilarities (default=" <i>add</i> "). For more details type "?metaMDS" into R command line.)
group	Table with group assignments. Use only one column. Use the first line as header. Assign the samples to groups in the next lines. The order and the number of these lines has to be identical to the order and the number of the samples printed in R. Use only integer values in the range from 1 to 25.
main	Character string used as title of the NMDS plot (default="")
type	Type of the plot (default=" <i>p</i> "). The "p" indicates points. For more details type "?points" into R command line.
cex	numeric (default=0.6). Character expansion factor. Used for the final size of the characters.

pos	Position of the text (default=4). Values of 1, 2, 3 and 4 indicate positions below, to the left of, above and to the right of the specified coordinates, respectively.
shrink	logical (default=TRUE). Shrink back species scores if they were expanded originally.
legend_pos	Position of the legend (default="topleft"). For more details type "?legend" into R command line.
pch	Plotting symbol (default=1) if group is FALSE. For more details type "?points" into R command line.
col	Color of the symbols and lines within the plot (default="black") if group is FALSE. Can be a color code or a name.
abiotic	Table with abiotic data. Should be a tab-delimited text file using '.' as decimal delimiter. Use one row for one sample and one column for one abiotic parameter. Use the first column for the first parameter and the first line as header. The order and the number of the lines have to be identical to the order and the number of the samples printed in R.
p.max	Decimal number defining the significance level of the abiotic parameters (default=0.05) if abiotic =TRUE. Only parameters less/equal this value are plotted.
col_abiotic	Color used for the plotted abiotic parameters (default="magenta").
verbose	logical (default=FALSE). Change to TRUE to print results of the metaMDS function and the p-values of the abiotic parameters.
...	Additional parameters used for the plot and the metaMDS function. For more details type "?plot", "?points", "?text" or "?metaMDS" into R command line.

Details

Visualizes the distance between samples based on their cytometrically measured cell abundance information using nonmetric multidimensional scaling (NMDS). NMDS is a mathematical technique to visualize the distances between objects (the samples, in this case). The distances within the plot are used to be in accordance with the dis-/similarities of the samples. The NMDS plot can be created using either the relative/percental cell numbers or the normalized values. If there are high abundance and low abundance gates the NMDS plot could be distorted. In this case it is better to use the normalized values. See reference Koch et al. 2013, Box 1 for more details. The NMDS analysis is performed by using the metaMDS function of the R package "vegan" (see reference Warnes et al. 2013).

Author(s)

Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Susanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <info.fetzer@stockholmresilience.su.se>, Susann Müller <susann.mueller@ufz.de>

References

Koch, Christin and Günther, Susanne and Desta, Adey Feleke and Hübschmann, Thomas and Müller, Susann (2013). Cytometric fingerprinting for analysing microbial intra-community structure variation and identifying sub-community function. *Nature Protocols*, 8(1):190-202,

Gregory R. Warnes, Ben Bolker, Lodewijk Bonebakker, Robert Gentleman, Wolfgang Huber, Andy Liaw, Thomas Lumley, Martin Maechler, Arni Magnusson, Steffen Moeller, Marc Schwartz and Bill Venables (2013). gplots: Various R programming tools for plotting data. R package version 2.12.1. <http://CRAN.R-project.org/package=gplots>

Examples

```
require(vegan)

## Show the NMDS plot of the normalized cell numbers

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
nmds(Normalized_mean)

## Change the title of the plot to "NMDS normalized", use triangles as plotting
## symbols, change the color to red and position the text below the triangles
## Use a dotted line (lty=3)

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
nmds(Normalized_mean,main="NMDS normalized",type="b",pos=1,pch=2,col="red",lty=3)

## Plot sample groups saved as data frame groups
## Print additional information

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
groups<-data.frame("groups"=c(1,1,1,1,2,3,3,3,3,3))
nmds(Normalized_mean,group=groups,main="NMDS normalized",verbose=TRUE)

## Plot additional gate information and
## abiotic parameters saved in dataset Abiotic_data_sample

data(Cell_number_sample)
Normalized_mean<-normalize(Cell_number_sample[,-1],digits=2)
Normalized_mean<-data.frame(data.matrix(Normalized_mean))
groups<-data.frame("groups"=c(1,1,1,1,2,3,3,3,3,3))
data(Abiotic_data_sample)
nmds(Normalized_mean,group=groups,main="NMDS normalized",
abiotic=Abiotic_data_sample[,-1],verbose=TRUE)
```

Description

Normalize the relative or percental cell numbers.

Usage

```
## S4 method for signature 'data.frame'
normalize(x,method="mean",show_avg=TRUE,...)

## S4 method for signature 'matrix'
normalize(x,method="mean",show_avg=TRUE,...)
```

Arguments

<code>x</code>	Data frame or matrix of all relative or percental cell numbers. Use one row per sample and one column per gate. Use the first column for the first gate. If your first column is used e.g. for sample names read the manual before you continue. The names of the gates may not contain any whitespace. If the values contain commas they must be expressed as ".". Missing values or NA's are allowed but should be expressed as "NA" or empty entries within the table.
<code>method</code>	Character string indicating which method is used for normalization (default="mean"). Can be changed to "first". See Details for further information.
<code>show_avg</code>	logical (default=TRUE). Show average values. Can be changed to FALSE if the averages are not of interest. Averages are only shown if method ="mean".
<code>...</code>	Additional parameters used for printing and writing e.g. number of digits.

Details

This step should be done to ensure the comparability of gates with highly different (low and high) cell abundances. There are two different methods to do this. By choosing "mean" the individual cell number of each gate is normalized by dividing the relative value by the mean of the relative or percental cell numbers for that gate. By choosing "first" the individual cell number of each gate is normalized by dividing the relative value by the first value of that gate.

Author(s)

Joachim Schumann <joachim.schumann@ufz.de>, Christin Koch <christin.koch@ufz.de>, Susanne Günther <susanne.guenther@ufz.de>, Ingo Fetzer <info.fetzer@stockholmresilience.su.se>, Susann Müller <susann.mueller@ufz.de>

Examples

```
## Normalize the percental cell numbers saved in dataset Cell_number_sample
## Use the default method and show the averages with two digits
## Note that the averages are very different but the normalized values
## are in the same range

data(Cell_number_sample)
normalize(Cell_number_sample[,-1],digits=2)
```

```
## Use the method "first"
## Print normalized values
## After normalization the first value of every gate is 1.00

data(Cell_number_sample)
normalize(Cell_number_sample[,-1],method="first",digits=2)
```

Index

- * **barcode,normalize**
 - cybar_plot, 6
- * **correlation**
 - correlation, 3
- * **datasets**
 - Abiotic_data_sample, 3
 - Cell_number_sample, 3
 - Corr_data_sample, 5
- *
 - file.show(file.path(R.home(doc),KEYWORDS))**
 - correlation, 3
 - cybar_plot, 6
 - nmDS, 9
 - normalize, 11
- * **nmDS,normalize**
 - nmDS, 9
- * **normalize**
 - normalize, 11

Abiotic_data_sample, 3

Cell_number_sample, 3

Corr_data_sample, 5

correlation, 3

correlation,data.frame-method
(correlation), 3

correlation,matrix-method
(correlation), 3

cybar_plot, 6

cybar_plot,data.frame,data.frame-method
(cybar_plot), 6

cybar_plot,data.frame,matrix-method
(cybar_plot), 6

cybar_plot,data.frame,missing-method
(cybar_plot), 6

cybar_plot,matrix,data.frame-method
(cybar_plot), 6

cybar_plot,matrix,matrix-method
(cybar_plot), 6

cybar_plot,matrix,missing-method
(cybar_plot), 6

cybar_plot,missing,data.frame-method
(cybar_plot), 6

cybar_plot,missing,matrix-method
(cybar_plot), 6

flowCyBar (flowCyBar-package), 2

flowCyBar-package, 2

nmDS, 9

nmDS,data.frame-method (nmDS), 9

nmDS,matrix-method (nmDS), 9

normalize, 11

normalize,data.frame-method
(normalize), 11

normalize,matrix-method (normalize), 11