# Package 'pcaMethods'

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Title A collection of PCA methods

LinkingTo Rcpp LazyLoad Yes

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SystemRequirements Rcpp

Description Provides Bayesian PCA, Probabilistic PCA, Nipals PCA, Inverse Non-Linear PCA and the conventional SVD PCA. A cluster based method for missing value estimation is included for comparison. BPCA, PPCA and NipalsPCA may be used to perform PCA on incomplete data as well as for accurate missing value estimation. A set of methods for printing and plotting the results is also provided. All PCA methods make use of the same data structure (pcaRes) to provide a common interface to the PCA results. Initiated at the Max-Planck Institute for Molecular Plant Physiology, Golm, Germany.

**Version** 1.96.0

URL https://github.com/hredestig/pcamethods

BugReports https://github.com/hredestig/pcamethods/issues

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'AllGenerics.R' 'BPCA\_dostep.R' 'BPCA\_initmodel.R' 'bpca.R'

'checkData.R' 'forkNlpcaNet.R' 'kEstimate.R' 'kEstimateFast.R'

'lineSearch.R' 'llsImpute.R' 'methods-ExpressionSet.R'

'methods-nniRes.R' 'methods-pcaRes.R' 'nipalsPca.R' 'nlpca.R'

'optiAlgCgd.R' 'orth.R' 'pca.R' 'pcaMethods-package.R' 'ppca.R'

'prep.R' 'repmat.R' 'robustPca.R' 'sortFeatures.R'

'svdImpute.R' 'vector2matrices.R' 'xval.R'

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asExprSet

Convert pcaRes object to an expression set

### **Description**

This function can be used to conveniently replace the expression matrix in an ExpressionSet with the completed data from a pcaRes object.

# Usage

```
asExprSet(object, exprSet)
```

# Arguments

object pcaRes – The object containing the completed data.

exprSet ExpressionSet – The object passed on to pca for missing value estimation.

#### **Details**

This is not a standard as function as pcaRes object alone not can be converted to an ExpressionSet (the pcaRes object does not hold any phenoData for example).

#### Value

An object without missing values of class ExpressionSet.

### Author(s)

Wolfram Stacklies

CAS-MPG Partner Institute for Computational Biology, Shanghai, China

biplot-methods

Plot a overlaid scores and loadings plot

### **Description**

Visualize two-components simultaneously

### Usage

```
## S3 method for class 'pcaRes'
biplot(x, choices = 1:2, scale = 1,
    pc.biplot = FALSE, ...)

## S4 method for signature 'pcaRes'
biplot(x, choices = 1:2, scale = 1,
    pc.biplot = FALSE, ...)
```

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#### **Arguments**

a pcaRes object choices which two pcs to plot The variables are scaled by  $\lambda^{scale}$  and the observations are scaled by  $\lambda^{scale}$ scale where lambda are the singular values as computed by princomp. Normally  $0 \le scale \le 1$ , and a warning will be issued if the specified 'scale' is outside this range. pc.biplot If true, use what Gabriel (1971) refers to as a "principal component biplot", with  $\lambda = 1$  and observations scaled up by sqrt(n) and variables scaled down by

sqrt(n). Then the inner products between variables approximate covariances and

distances between observations approximate Mahalanobis distance.

optional arguments to be passed to biplot.default.

#### **Details**

This is a method for the generic function 'biplot'. There is considerable confusion over the precise definitions: those of the original paper, Gabriel (1971), are followed here. Gabriel and Odoroff (1990) use the same definitions, but their plots actually correspond to pc.biplot = TRUE.

#### Value

a plot is produced on the current graphics device.

#### Author(s)

Kevin Wright, Adapted from biplot.prcomp

### See Also

```
prcomp, pca, princomp
```

#### **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4])</pre>
biplot(pcIr)
```

bpca

Bayesian PCA missing value estimation

## **Description**

Implements a Bayesian PCA missing value estimator. The script is a port of the Matlab version provided by Shigeyuki OBA. See also http://ishiilab.jp/member/oba/tools/BPCAFill.html. BPCA combines an EM approach for PCA with a Bayesian model. In standard PCA data far from the training set but close to the principal subspace may have the same reconstruction error. BPCA defines a likelihood function such that the likelihood for data far from the training set is much lower, even if they are close to the principal subspace.

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#### **Usage**

```
bpca(Matrix, nPcs = 2, maxSteps = 100, verbose = interactive(),
  threshold = 1e-04, ...)
```

#### Arguments

Matrix matrix - Pre-processed matrix (centered, scaled) with variables in columns and observations in rows. The data may contain missing values, denoted as NA. nPcs numeric - Number of components used for re-estimation. Choosing few components may decrease the estimation precision. numeric – Maximum number of estimation steps. maxSteps verbose boolean – BPCA prints the number of steps and the increase in precision if set

to TRUE. Default is interactive().

threshold convergence threshold

Reserved for future use. Currently no further parameters are used

#### **Details**

Scores and loadings obtained with Bayesian PCA slightly differ from those obtained with conventional PCA. This is because BPCA was developed especially for missing value estimation. The algorithm does not force orthogonality between factor loadings, as a result factor loadings are not necessarily orthogonal. However, the BPCA authors found that including an orthogonality criterion made the predictions worse.

The authors also state that the difference between real and predicted Eigenvalues becomes larger when the number of observation is smaller, because it reflects the lack of information to accurately determine true factor loadings from the limited and noisy data. As a result, weights of factors to predict missing values are not the same as with conventional PCA, but the missing value estimation is improved.

BPCA works iteratively, the complexity is growing with  $O(n^3)$  because several matrix inversions are required. The size of the matrices to invert depends on the number of components used for re-estimation.

Finding the optimal number of components for estimation is not a trivial task; the best choice depends on the internal structure of the data. A method called kEstimate is provided to estimate the optimal number of components via cross validation. In general few components are sufficient for reasonable estimation accuracy. See also the package documentation for further discussion about on what data PCA-based missing value estimation makes sense.

It is not recommended to use this function directly but rather to use the pca() wrapper function.

There is a difference with respect the interpretation of rows (observations) and columns (variables) compared to matlab implementation. For estimation of missing values for microarray data, the suggestion in the original bpca is to intepret genes as observations and the samples as variables. In pcaMethods however, genes are interpreted as variables and samples as observations which arguably also is the more natural interpretation. For bpca behavior like in the matlab implementation, simply transpose your input matrix.

Details about the probabilistic model underlying BPCA are found in Oba et. al 2003. The algorithm uses an expectation maximation approach together with a Bayesian model to approximate the bpca 7

principal axes (eigenvectors of the covariance matrix in PCA). The estimation is done iteratively, the algorithm terminates if either the maximum number of iterations was reached or if the estimated increase in precision falls below  $1e^{-4}$ .

**Complexity:** The relatively high complexity of the method is a result of several matrix inversions required in each step. Considering the case that the maximum number of iteration steps is needed, the approximate complexity is given by the term

$$maxSteps \cdot row_{miss} \cdot O(n^3)$$

Where  $row_{miss}$  is the number of rows containing missing values and  $O(n^3)$  is the complexity for inverting a matrix of size components. Components is the number of components used for re-estimation.

#### Value

Standard PCA result object used by all PCA-based methods of this package. Contains scores, loadings, data mean and more. See pcaRes for details.

#### Note

Requires MASS.

#### Author(s)

Wolfram Stacklies

#### References

Shigeyuki Oba, Masa-aki Sato, Ichiro Takemasa, Morito Monden, Ken-ichi Matsubara and Shin Ishii. A Bayesian missing value estimation method for gene expression profile data. *Bioinformatics*, 19(16):2088-2096, Nov 2003.

#### See Also

ppca, svdImpute, prcomp, nipalsPca, pca, pcaRes. kEstimate.

#### **Examples**

```
## Load a sample metabolite dataset with 5\% missig values (metaboliteData)e
data(metaboliteData)
## Perform Bayesian PCA with 2 components
pc <- pca(t(metaboliteData), method="bpca", nPcs=2)
## Get the estimated principal axes (loadings)
loadings <- loadings(pc)
## Get the estimated scores
scores <- scores(pc)
## Get the estimated complete observations
cObs <- completeObs(pc)
## Now make a scores and loadings plot
slplot(pc)</pre>
```

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BPCA\_dostep

Do BPCA estimation step

### **Description**

The function contains the actual implementation of the BPCA component estimation. It performs one step of the BPCA EM algorithm. It is called 'maxStep' times from within the main loop in BPCAestimate.

### Usage

```
BPCA_dostep(M, y)
```

### **Arguments**

М Data structure containing all needed information. See the source documentation

of BPCA\_initmodel for details

Numeric original data matrix У

# **Details**

This function is NOT intended to be run standalone.

### Value

Updated version of the data structure

### Author(s)

Wolfram Stacklies

BPCA\_initmodel

Initialize BPCA model

# **Description**

Model initialization for Bayesian PCA. This function is NOT inteded to be run separately!

### Usage

```
BPCA_initmodel(y, components)
```

# **Arguments**

numeric matrix containing missing values. Missing values are denoted as 'NA' У

Number of components used for estimation components

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### **Details**

The function calculates the initial Eigenvectors by use of SVD from the complete rows. The data structure M is created and initial values are assigned.

#### Value

### List containing

rows Row number of input matrix
cols Column number of input matrix
comps Number of components to use

yest (working variable) current estimate of complete data row\_miss (Array) Indizes of rows containing missing values

row\_nomiss (Array) Indices of complete rows (such with no missing values)

nans Matrix of same size as input data. TRUE if input == NA, false otherwise

mean Column wise data mean

PA (d x k) Estimated principal axes (eigenvectors, loadings) The matrix ROWS are

the vectors

tau Estimated precision of the residual error

scores Estimated scores

Further elements are: galpha0, balpha0, alpha, gmu0, btau0, gtau0, SigW. These are working variables or constants.

### Author(s)

Wolfram Stacklies

center, pcaRes-method Get the centers of the original variables

# Description

Get the centers of the original variables

# Usage

```
center(object, ...)
```

# Arguments

object pcaRes object
... Not used

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# Value

Vector with the centers

# Author(s)

Henning Redestig

centered, pcaRes-method

Check centering was part of the model

# Description

Check centering was part of the model

# Usage

```
centered(object, ...)
```

# **Arguments**

object pcaRes object
... Not used

### Value

TRUE if model was centered

### Author(s)

Henning Redestig

checkData

Do some basic checks on a given data matrix

# Description

Check a given data matrix for consistency with the format required for further analysis. The data must be a numeric matrix and not contain:

- Inf values
- NaN values
- Rows or columns that consist of NA only

### Usage

```
checkData(data, verbose = FALSE)
```

### **Arguments**

data matrix – Data to check.

verbose boolean – If TRUE, the function prints messages whenever an error in the data

set is found.

#### Value

isValid

boolean – TRUE if no errors were found, FALSE otherwise. is Valid contains a set of attributes, these are:

- isNumeric TRUE if data is numeric, false otherwise
- isInfinite TRUE if data contains 'Inf' values, false otherwise
- isNaN TRUE if data contains 'NaN' values, false otherwise
- isMatrix TRUE if the data is in matrix format, FALSE otherwise
- naRows TRUE if data contains rows in which all elements are 'NA', FALSE otherwise
- naCols TRUE if data contains columns in which all elements are 'NA', FALSE otherwise

# Author(s)

Wolfram Stacklies

completeObs,nniRes-method

Get the original data with missing values replaced with predicted values.

## Description

Get the original data with missing values replaced with predicted values.

### Usage

```
completeObs(object, ...)
```

# **Arguments**

object to fetch complete data from

... Not used

### Value

Completed data (matrix)

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### Author(s)

Henning Redestig

cvseg

Get CV segments

# Description

Get cross-validation segments that have (as far as possible) the same ratio of all classes (if classes are present)

# Usage

```
cvseg(x, fold = 7, seed = NULL)
```

# Arguments

| Х    | a factor, character or numeric vector that describes class membership of a set of items, or, a numeric vector indicating unique indices of items, or, a numeric of length 1 that describes the number of items to segment (without any classes) |
|------|---|
| fold | the desired number of segments  |

seed randomization seed for reproducibility

# Value

a list where each element is a set of indices that defines the CV segment.

# Author(s)

Henning Redestig

### See Also

the cvsegments function in the pls package

# Examples

```
seg <- cvseg(iris$Species, 10)
sapply(seg, function(s) table(iris$Species[s]))
cvseg(20, 10)</pre>
```

cvstat,pcaRes-method 13

cvstat, pcaRes-method  $Get\ cross-validation\ statistics\ (e.g.\ Q^2).$ 

# **Description**

Get cross-validation statistics (e.g.  $Q^2$ ).

# Usage

```
cvstat(object, ...)
```

# **Arguments**

object pcaRes object ... not used

#### Value

vector CV statistics

### Author(s)

Henning Redestig

deletediagonals

Delete diagonals

# **Description**

Replace a diagonal of elements of a matrix with NA

# Usage

```
deletediagonals(x, diagonals = 1)
```

# **Arguments**

x The matrix

diagonals The diagonal to be replaced, i.e. the first, second and so on when looking at the

fat version of the matrix (transposed or not) counting from the bottom. Can be

a vector to delete more than one diagonal.

### **Details**

Used for creating artifical missing values in matrices without causing any full row or column to be completely missing

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# Value

The original matrix with some values missing

# Author(s)

Henning Redestig

derrorHierarchic

Later

# Description

Later

# Usage

```
derrorHierarchic(nlnet, trainIn, trainOut)
```

# Arguments

nlnet the nlnet
trainIn training data
trainOut fitted data

### Value

derror

# Author(s)

Henning Redestig, Matthias Scholz

dim.pcaRes

Dimensions of a PCA model

# **Description**

Dimensions of a PCA model

# Usage

```
## S3 method for class 'pcaRes' \dim(x)
```

#### **Arguments**

x a pcaRes object

#### Value

Get the dimensions of this PCA model

#### Author(s)

Henning Redestig

DModX, pcaRes-method DModX

# Description

Distance to the model of X-space.

# Usage

```
DModX(object, dat, newdata=FALSE, type=c("normalized", "absolute"), ...)
```

### **Arguments**

object a pcaRes object

dat the original data, taken from completeObs if left missing.

newdata logical indicating if this data was part of the training data or not. If it was, it is

adjusted by a near one factor  $v = (N/(N - A - A0))^{-1}$ 

type if absolute or normalized values should be given. Normalized values are ad-

justed to the the total RSD of the model.

... Not used

#### **Details**

Measures how well described the observations are, i.e. how well they fit in the mode. High DModX indicate a poor fit. Defined as:

$$\frac{\sqrt{\frac{SSE_i}{K-A}}}{\sqrt{\frac{SSE}{(N-A-A_0)(K-A)}}}$$

For observation i, in a model with A components, K variables and N observations. SSE is the squared sum of the residuals.  $A_0$  is 1 if model was centered and 0 otherwise. DModX is claimed to be approximately F-distributed and can therefore be used to check if an observation is significantly far away from the PCA model assuming normally distributed data.

Pass original data as an argument if the model was calculated with completeObs=FALSE.

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# Value

A vector with distances from observations to the PCA model

# Author(s)

Henning Redestig

### References

Introduction to Multi- and Megavariate Data Analysis using Projection Methods (PCA and PLS), L. Eriksson, E. Johansson, N. Kettaneh-Wold and S. Wold, Umetrics 1999, p. 468

# **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4])
with(iris, plot(DModX(pcIr)~Species))</pre>
```

errorHierarchic

Later

# Description

Later

# Usage

```
errorHierarchic(nlnet, trainIn, trainOut)
```

# **Arguments**

nlnet The nlnet
trainIn training data
trainOut fitted data

# Value

error

# Author(s)

Henning Redestig, Matthias Scholz

fitted-methods 17

Extract fitted values from PCA.

# **Description**

Fitted values of a PCA model

# Usage

```
## S3 method for class 'pcaRes'
fitted(object, data = NULL, nPcs = nP(object),
    pre = TRUE, post = TRUE, ...)
## S4 method for signature 'pcaRes'
fitted(object, data = NULL, nPcs = nP(object),
    pre = TRUE, post = TRUE, ...)
```

# **Arguments**

| object | the pcaRes object of interest.   |
|--------|--|
| data   | For standard PCA methods this can safely be left null to get scores x loadings but if set, then the scores are obtained by projecting provided data onto the loadings. If data contains missing values the result will be all NA. Non-linear PCA is an exception, here if data is NULL then data is set to the completeObs and propaged through the network. |
| nPcs   | The number of PC's to consider   |
| pre    | pre-process data based on the pre-processing chosen for the PCA model  |
| post   | unpre-process the final data (add the center back etc to get the final estimate)   |
|        | Not used   |

## **Details**

This function extracts the fitted values from a pcaResobject. For PCA methods like SVD, Nipals, PPCA etc this is basically just the scores multipled by the loadings and adjusted for pre-processing. for non-linear PCA the original data is propagated through the network to obtain the approximated data.

### Value

A matrix representing the fitted data

### Author(s)

Henning Redestig

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# **Examples**

```
pc <- pca(iris[,1:4], nPcs=4, center=TRUE, scale="uv")
sum( (fitted(pc) - iris[,1:4])^2 )</pre>
```

forkNlpcaNet

Complete copy of nlpca net object

# **Description**

Complete copy of nlpca net object

# Usage

forkNlpcaNet(nlnet)

# Arguments

nlnet

a nlnet

### Value

A copy of the input nlnet

# Author(s)

Henning Redestig

getHierarchicIdx

*Index in hiearchy* 

# Description

Index in hiearchy

# Usage

```
getHierarchicIdx(hierarchicNum)
```

# **Arguments**

hierarchicNum A number

# Value

...

# Author(s)

Henning Redestig, Matthias Scholz

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helix

A helix structured toy data set

# Description

Simulated data set looking like a helix

# Usage

```
data(helix)
```

### **Details**

A matrix containing 1000 observations (rows) and three variables (columns).

#### Author(s)

Henning Redestig

# References

Matthias Scholz, Fatma Kaplan, Charles L. Guy, Joachim Kopka and Joachim Selbig. - Non-linear PCA: a missing data approach. *Bioinformatics* 2005 21(20):3887-3895

kEstimate

Estimate best number of Components for missing value estimation

# Description

Perform cross validation to estimate the optimal number of components for missing value estimation. Cross validation is done for the complete subset of a variable.

# Usage

```
kEstimate(Matrix, method = "ppca", evalPcs = 1:3, segs = 3,
  nruncv = 5, em = "q2", allVariables = FALSE,
  verbose = interactive(), ...)
```

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### **Arguments**

Matrix matrix – numeric matrix containing observations in rows and variables in columns

method character – of the methods found with pcaMethods() The option llsImputeAll

calls llsImpute with the allVariables = TRUE parameter.

evalPcs numeric – The principal components to use for cross validation or the number

of neighbour variables if used with llsImpute. Should be an array containing integer values, eg. evalPcs = 1:10 or evalPcs = c(2,5,8). The NRMSEP or

Q2 is calculated for each component.

segs numeric – number of segments for cross validation

nruncv numeric – Times the whole cross validation is repeated em character – The error measure. This can be nrmsep or q2

all Variables boolean – If TRUE, the NRMSEP is calculated for all variables, If FALSE, only

the incomplete ones are included. You maybe want to do this to compare several

methods on a complete data set.

verbose boolean - If TRUE, some output like the variable indexes are printed to the

console each iteration.

... Further arguments to pca or nni

#### **Details**

The assumption hereby is that variables that are highly correlated in a distinct region (here the non-missing observations) are also correlated in another (here the missing observations). This also implies that the complete subset must be large enough to be representative. For each incomplete variable, the available values are divided into a user defined number of cv-segments. The segments have equal size, but are chosen from a random equal distribution. The non-missing values of the variable are covered completely. PPCA, BPCA, SVDimpute, Nipals PCA, llsImpute an NLPCA may be used for imputation.

The whole cross validation is repeated several times so, depending on the parameters, the calculations can take very long time. As error measure the NRMSEP (see Feten et. al, 2005) or the Q2 distance is used. The NRMSEP basically normalises the RMSD between original data and estimate by the variable-wise variance. The reason for this is that a higher variance will generally lead to a higher estimation error. If the number of samples is small, the variable - wise variance may become an unstable criterion and the Q2 distance should be used instead. Also if variance normalisation was applied previously.

The method proceeds variable - wise, the NRMSEP / Q2 distance is calculated for each incomplete variable and averaged afterwards. This allows to easily see for wich set of variables missing value imputation makes senes and for wich set no imputation or something like mean-imputation should be used. Use kEstimateFast or Q2 if you are not interested in variable wise CV performance estimates.

Run time may be very high on large data sets. Especially when used with complex methods like BPCA or Nipals PCA. For PPCA, BPCA, Nipals PCA and NLPCA the estimation method is called  $(v_{miss} \cdot segs \cdot nruncv \cdot)$  times as the error for all numbers of principal components can be calculated at once. For LLSimpute and SVDimpute this is not possible, and the method is called  $(v_{miss} \cdot segs \cdot nruncv \cdot length(evalPcs))$  times. This should still be fast for LLSimpute because the method

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allows to choose to only do the estimation for one particular variable. This saves a lot of iterations. Here,  $v_{miss}$  is the number of variables showing missing values.

As cross validation is done variable-wise, in this function Q2 is defined on single variables, not on the entire data set. This is Q2 is calculated as as  $\frac{\sum (x-xe)^2}{\sum (x^2)}$ , where x is the currently used variable and xe it's estimate. The values are then averaged over all variables. The NRMSEP is already defined variable-wise. For a single variable it is then  $\sqrt{\left(\frac{\sum (x-xe)^2}{(n\cdot var(x))}\right)}$ , where x is the variable and xe it's estimate, n is the length of x. The variable wise estimation errors are returned in parameter variable-WiseError.

#### Value

A list with:

bestNPcs number of PCs or k for which the minimal average NRMSEP or the maximal

Q2 was obtained.

eError an array of of size length(evalPcs). Contains the average error of the cross vali-

dation runs for each number of components.

variableWiseError

Matrix of size incomplete\_variables x length(evalPcs). Contains the NRM-SEP or Q2 distance for each variable and each number of PCs. This allows to easily see for wich variables imputation makes sense and for which one it should

not be done or mean imputation should be used.

evalPcs The evaluated numbers of components or number of neighbours (the same as

the evalPcs input parameter).

variableIx Index of the incomplete variables. This can be used to map the variable wise

error to the original data.

#### Author(s)

Wolfram Stacklies

### See Also

```
kEstimateFast, Q2, pca, nni.
```

#### **Examples**

22 kEstimateFast

kEstimateFast

Estimate best number of Components for missing value estimation

### **Description**

This is a simple estimator for the optimal number of componets when applying PCA or LLSimpute for missing value estimation. No cross validation is performed, instead the estimation quality is defined as Matrix[!missing] - Estimate[!missing]. This will give a relatively rough estimate, but the number of iterations equals the length of the parameter evalPcs.

Does not work with LLSimpute!! As error measure the NRMSEP (see Feten et. al, 2005) or the Q2 distance is used. The NRMSEP basically normalises the RMSD between original data and estimate by the variable-wise variance. The reason for this is that a higher variance will generally lead to a higher estimation error. If the number of samples is small, the gene - wise variance may become an unstable criterion and the Q2 distance should be used instead. Also if variance normalisation was applied previously.

### Usage

```
kEstimateFast(Matrix, method = "ppca", evalPcs = 1:3, em = "nrmsep",
   allVariables = FALSE, verbose = interactive(), ...)
```

### **Arguments**

| Matrix       | matrix – numeric matrix containing observations in rows and variables in columns  |
|--------------|---|
| method       | character – a valid pca method (see pca).   |
| evalPcs      | numeric – The principal components to use for cross validation or cluster sizes if used with llsImpute. Should be an array containing integer values, eg. evalPcs = $1:10$ or evalPcs = $C(2,5,8)$ . The NRMSEP is calculated for each component. |
| em           | character – The error measure. This can be nrmsep or q2   |
| allVariables | boolean – If TRUE, the NRMSEP is calculated for all variables, If FALSE, only the incomplete ones are included. You maybe want to do this to compare several methods on a complete data set.  |
| verbose      | boolean – If TRUE, the NRMSEP and the variance are printed to the console each iteration.   |
|              | Further arguments to pca  |

### Value

list Returns a list with the elements:

- minNPcs number of PCs for which the minimal average NRMSEP was obtained
- eError an array of of size length(evalPcs). Contains the estimation error for each number of components.
- evalPcs The evaluated numbers of components or cluster sizes (the same as the evalPcs input parameter).

### Author(s)

Wolfram Stacklies

#### See Also

kEstimate.

### **Examples**

```
data(metaboliteData)
# Estimate best number of PCs with ppca for component 2:4
esti <- kEstimateFast(t(metaboliteData), method = "ppca", evalPcs = 2:4, em="nrmsep")
barplot(drop(esti$eError), xlab = "Components",ylab = "NRMSEP (1 iterations)")
# The best k value is:
print(esti$minNPcs)</pre>
```

leverage, pcaRes-method

Extract leverages of a PCA model

# **Description**

The leverages of PCA model indicate how much influence each observation has on the PCA model. Observations with high leverage has caused the principal components to rotate towards them. It can be used to extract both "unimportant" observations as well as picking potential outliers.

### Usage

```
## S4 method for signature 'pcaRes'
leverage(object)
```

# **Arguments**

object a pcaRes object

# **Details**

```
Defined as Tr(T(T'T)^{-1}T')
```

#### Value

The observation leverages as a numeric vector

# Author(s)

Henning Redestig

24 lineSearch

### References

Introduction to Multi- and Megavariate Data Analysis using Projection Methods (PCA and PLS), L. Eriksson, E. Johansson, N. Kettaneh-Wold and S. Wold, Umetrics 1999, p. 466

# **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4])
## versicolor has the lowest leverage
with(iris, plot(leverage(pcIr)~Species))</pre>
```

lineSearch

Line search for conjugate gradient

# **Description**

Line search for conjugate gradient

# Usage

```
lineSearch(nlnet, dw, e0, ttGuess, trainIn, trainOut, verbose)
```

# **Arguments**

nlnet The nlnet
dw ..
e0 ..
ttGuess ..

trainIn Training data trainOut Fitted data

verbose logical, print messages

### Value

•••

### Author(s)

Henning Redestig, Matthias Scholz

linr 25

linr

Linear kernel

### **Description**

Linear kernel

# Usage

linr(x)

# Arguments

Х

datum

### Value

Input value

# Author(s)

Henning Redestig, Matthias Scholz

listPcaMethods

List PCA methods

# **Description**

Vector with current valid PCA methods

# Usage

```
listPcaMethods(which = c("all", "linear", "nonlinear"))
```

# **Arguments**

which

the type of methods to get. E.g. only get the PCA methods based on the classical model where the fitted data is a direct multiplication of scores and loadings.

# Value

A character vector with the current methods for doing PCA

# Author(s)

Henning Redestig

26 IlsImpute

| llsImpute | LLSimpute algorithm |  |
|-----------|---------------------|--|
|           |                     |  |

# Description

Missing value estimation using local least squares (LLS). First, k variables (for Microarrya data usually the genes) are selected by pearson, spearman or kendall correlation coefficients. Then missing values are imputed by a linear combination of the k selected variables. The optimal combination is found by LLS regression. The method was first described by Kim et al, Bioinformatics, 21(2),2005.

# Usage

```
llsImpute(Matrix, k = 10, center = FALSE, completeObs = TRUE,
  correlation = "pearson", allVariables = FALSE, maxSteps = 100,
  xval = NULL, verbose = FALSE, ...)
```

# Arguments

| Matrix       | matrix – Data containing the variables (genes) in columns and observations (samples) in rows. The data may contain missing values, denoted as NA.  |
|--------------|--|
| k            | ${\tt numeric-Cluster\ size,\ this\ is\ the\ number\ of\ similar\ genes\ used\ for\ regression.}$  |
| center       | boolean – Mean center the data if TRUE   |
| completeObs  | boolean – Return the estimated complete observations if TRUE. This is the input data with NA values replaced by the estimated values.  |
| correlation  | character – How to calculate the distance between genes. One out of pearson $ $ kendall $ $ spearman , see also help("cor").   |
| allVariables | boolean – Use only complete genes to do the regression if TRUE, all genes if FALSE.  |
| maxSteps     | numeric – Maximum number of iteration steps if allGenes = TRUE.  |
| xval         | numeric Use LLSimpute for cross validation. xval is the index of the gene to estimate, all other incomplete genes will be ignored if this parameter is set. We do not consider them in the cross-validation. |
| verbose      | boolean – Print step number and relative change if TRUE and all<br>Variables = $\ensuremath{TRUE}$   |
|              | Reserved for parameters used in future version of the algorithm  |
|              |  |

### **Details**

Missing values are denoted as NA

It is not recommended to use this function directly but rather to use the nni() wrapper function. The methods provides two ways for missing value estimation, selected by the allVariables option. The first one is to use only complete variables for the regression. This is preferable when the number of incomplete variables is relatively small.

IlsImpute 27

The second way is to consider all variables as candidates for the regression. Hereby missing values are initially replaced by the columns wise mean. The method then iterates, using the current estimate as input for the regression until the change between new and old estimate falls below a threshold (0.001).

#### Value

nniRes

Standard nni (nearest neighbour imputation) result object of this package. See nniRes for details.

#### Note

Each step the generalized inverse of a miss x k matrix is calculated. Where miss is the number of missing values in variable j and k the number of neighbours. This may be slow for large values of k and / or many missing values. See also help("ginv").

### Author(s)

Wolfram Stacklies

### References

Kim, H. and Golub, G.H. and Park, H. - Missing value estimation for DNA microarray gene expression data: local least squares imputation. *Bioinformatics*, 2005; 21(2):187-198.

Troyanskaya O. and Cantor M. and Sherlock G. and Brown P. and Hastie T. and Tibshirani R. and Botstein D. and Altman RB. - Missing value estimation methods for DNA microarrays. *Bioinformatics*. 2001 Jun;17(6):520-525.

#### See Also

```
pca, nniRes, nni.
```

### **Examples**

```
## Load a sample metabolite dataset (metaboliteData) with already 5\% of
## data missing
data(metaboliteData)
## Perform llsImpute using k = 10
## Set allVariables TRUE because there are very few complete variables
result <- llsImpute(metaboliteData, k = 10, correlation="pearson", allVariables=TRUE)
## Get the estimated complete observations
cObs <- completeObs(result)</pre>
```

loadings,ANY-method

Crude way to unmask the function with the same name from stats

# Description

Crude way to unmask the function with the same name from stats

# Usage

```
## S4 method for signature 'ANY'
loadings(object, ...)
```

# Arguments

```
object any object ... not used
```

#### Value

The loadings

# Author(s)

Henning Redestig

```
loadings,pcaRes-method
```

Get loadings from a pcaRes object

# Description

Get loadings from a pcaRes object

## Usage

```
## S4 method for signature 'pcaRes'
loadings(object, ...)
```

# **Arguments**

```
object a pcaRes object ... not used
```

# Value

The loadings as a matrix

loadings.pcaRes 29

### Author(s)

Henning Redestig

#### See Also

loadings.pcaRes

loadings.pcaRes

Get loadings from a pcaRes object

# **Description**

Get loadings from a pcaRes object

# Usage

```
## S3 method for class 'pcaRes'
loadings(object, ...)
```

# Arguments

object a pcaRes object ... not used

#### Value

The loadings as a matrix

### Author(s)

Henning Redestig

metaboliteData

A incomplete metabolite data set from an Arabidopsis coldstress experiment

# **Description**

A incomplete subset from a larger metabolite data set. This is the original, complete data set and can be used to compare estimation results created with the also provided incomplete data (called metaboliteData).

### **Details**

A matrix containing 154 observations (rows) and 52 metabolites (columns). The data contains 5% of artificially created uniformly distributed misssing values. The data was created during an in house Arabidopsis coldstress experiment.

### Author(s)

Wolfram Stacklies

#### References

Matthias Scholz, Fatma Kaplan, Charles L. Guy, Joachim Kopka and Joachim Selbig. - Non-linear PCA: a missing data approach. *Bioinformatics* 2005 21(20):3887-3895

#### See Also

metaboliteDataComplete

metaboliteDataComplete

A complete metabolite data set from an Arabidopsis coldstress experiment

# Description

A complete subset from a larger metabolite data set. This is the original, complete data set and can be used to compare estimation results created with the also provided incomplete data (called metaboliteData). The data was created during an in house Arabidopsis coldstress experiment.

### **Details**

A matrix containing 154 observations (rows) and 52 metabolites (columns).

# Author(s)

Wolfram Stacklies

#### References

Matthias Scholz, Fatma Kaplan, Charles L. Guy, Joachim Kopka and Joachim Selbig. - Non-linear PCA: a missing data approach. *Bioinformatics* 2005 21(20):3887-3895

#### See Also

metaboliteData

method, pcaRes-method Get the used PCA method

# **Description**

Get the used PCA method

# Usage

```
method(object, ...)
```

# **Arguments**

pcaRes object object Not used . . .

#### Value

The used pca method

## Author(s)

Henning Redestig

nipalsPca

NIPALS PCA

# Description

PCA by non-linear iterative partial least squares

# Usage

```
nipalsPca(Matrix, nPcs = 2, varLimit = 1, maxSteps = 5000,
  threshold = 1e-06, ...)
```

### **Arguments**

| Matrix   | as columns.  |
|----------|--|
| nPcs     | Number of components that should be extracted.   |
| varLimit | Optionally the ratio of variance that should be explained. nPcs is ignored if $varLimit < 1$ |
| maxSteps | Defines how many iterations can be done before algorithm should abort (hap-                  |

pens almost exclusively when there were some wrong in the input data).

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threshold The limit condition for judging if the algorithm has converged or not, specifically if a new iteration is done if  $(T_{old} - T)^T (T_{old} - T) > 1$ imit.

Only used for passing through arguments.

### **Details**

Can be used for computing PCA on a numeric matrix using either the NIPALS algorithm which is an iterative approach for estimating the principal components extracting them one at a time. NIPALS can handle a small amount of missing values. It is not recommended to use this function directly but rather to use the pca() wrapper function.

#### Value

A pcaRes object.

#### Author(s)

Henning Redestig

#### References

Wold, H. (1966) Estimation of principal components and related models by iterative least squares. In Multivariate Analysis (Ed., P.R. Krishnaiah), Academic Press, NY, 391-420.

#### See Also

```
prcomp, princomp, pca
```

### **Examples**

```
data(metaboliteData)
mat <- prep(t(metaboliteData))
pc <- nipalsPca(mat, nPcs=2)
## better use pca()
pc <- pca(t(metaboliteData), method="nipals", nPcs=2)</pre>
```

nlpca

Non-linear PCA

# Description

Neural network based non-linear PCA

### Usage

```
nlpca(Matrix, nPcs = 2, maxSteps = 2 * prod(dim(Matrix)),
  unitsPerLayer = NULL, functionsPerLayer = NULL,
  weightDecay = 0.001, weights = NULL, verbose = interactive(), ...)
```

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### **Arguments**

Matrix — Preprocessed data with the variables in columns and observations in

rows. The data may contain missing values, denoted as NA

nPcs numeric – Number of components to estimate. The preciseness of the missing

value estimation depends on thenumber of components, which should resemble

the internal structure of the data.

maxSteps numeric – Number of estimation steps. Default is based on a generous rule of

thumb.

unitsPerLayer The network units, example: c(2,4,6) for two input units 2 feature units (principal

components), one hidden layer fornon-linearity and three output units (original

amount ofvariables).

functionsPerLayer

The function to apply at each layer eg. c("linr", "tanh", "linr")

weightDecay Value between 0 and 1.

weights Starting weights for the network. Defaults to uniform random values but can be

set specifically to make algorithm deterministic.

verbose boolean - nlpca prints the number of steps and warning messages if set to

TRUE. Default is interactive().

... Reserved for future use. Not passed on anywhere.

#### **Details**

Artificial Neural Network (MLP) for performing non-linear PCA. Non-linear PCA is conceptually similar to classical PCA but theoretically quite different. Instead of simply decomposing our matrix (X) to scores (T) loadings (P) and an error (E) we train a neural network (our loadings) to find a curve through the multidimensional space of X that describes a much variance as possible. Classical ways of interpreting PCA results are thus not applicable to NLPCA since the loadings are hidden in the network. However, the scores of components that lead to low cross-validation errors can still be interpreted via the score plot. Unfortunately this method depend on slow iterations which currently are implemented in R only making this method extremely slow. Furthermore, the algorithm does not by itself decide when it has converged but simply does 'maxSteps' iterations.

### Value

Standard PCA result object used by all PCA-basedmethods of this package. Contains scores, loadings, data meanand more. See pcaRes for details.

#### Author(s)

Based on a matlab script by Matthias Scholz and ported to R by Henning Redestig

#### References

Matthias Scholz, Fatma Kaplan, Charles L Guy, Joachim Kopkaand Joachim Selbig. Non-linear PCA: a missing data approach. *Bioinformatics*, 21(20):3887-3895, Oct 2005

### **Examples**

```
## Data set with three variables where data points constitute a helix
data(helix)
helixNA <- helix
## not a single complete observation
helixNA <- t(apply(helix, 1, function(x) { x[sample(1:3, 1)] <- NA; x}))
## 50 steps is not enough, for good estimation use 1000
helixNlPca <- pca(helixNA, nPcs=1, method="nlpca", maxSteps=50)
fittedData <- fitted(helixNlPca, helixNA)
plot(fittedData[which(is.na(helixNA))], helix[which(is.na(helixNA))])
## compared to solution by Nipals PCA which cannot extract non-linear patterns
helixNipPca <- pca(helixNA, nPcs=2)
fittedData <- fitted(helixNipPca)
plot(fittedData[which(is.na(helixNA))], helix[which(is.na(helixNA))])</pre>
```

nmissing,pcaRes-method

Missing values

# Description

Missing values

#### Usage

```
nmissing(object, ...)
```

# **Arguments**

object pcaRes object ... Not used

#### Value

Get the number of missing values

## Author(s)

Henning Redestig

nni 35

| n | n | ٦ |
|---|---|---|
|   |   | ч |

Nearest neighbour imputation

# Description

Wrapper function for imputation methods based on nearest neighbour clustering. Currently llsImpute only.

# Usage

```
nni(object, method = c("llsImpute"), subset = numeric(), ...)
```

# Arguments

| object | Numerical matrix with (or an object coercible to such) with samples in rows and variables as columns. Also takes ExpressionSet in which case the transposed expression matrix is used. |
|--------|--|
| method | For convenience one can pass a large matrix but only use the variable specified as subset. Can be colnames or indices.   |
| subset | Currently "llsImpute" only.  |
|        | Further arguments to the chosen method.  |

## **Details**

This method is wrapper function to llsImpute, See documentation for link{llsImpute}.

# Value

A clusterRes object. Or a list containing a clusterRes object as first and an ExpressionSet object as second entry if the input was of type ExpressionSet.

# Author(s)

Wolfram Stacklies

# See Also

```
llsImpute, pca
```

# **Examples**

```
data(metaboliteData)
llsRes <- nni(metaboliteData, k=6, method="llsImpute", allGenes=TRUE)</pre>
```

36 nniRes

nniRes

Class for representing a nearest neighbour imputation result

### **Description**

This is a class representation of nearest neighbour imputation (nni) result

#### **Details**

# **Creating Objects**

new("nniRes", completeObs=[the estimated complete observations], k=[cluster size], nObs=[amount
of observations], nVar=[amount of variables], centered=[was the data centered befor running
LLSimpute], center=[original means], method=[method used to perform clustering], missing=[amount
of NAs])

#### **Slots**

```
completeObs "matrix", the estimated complete observations
nObs "numeric", amount of observations
nVar "numeric", amount of variables
correlation "character", the correlation method used (pearson, kendall or spearman)
centered "logical", data was centered or not
center "numeric", the original variable centers
k "numeric", cluster size
method "character", the method used to perform the clustering
missing "numeric", the total amount of missing values in original data
Methods
print Print function
```

# Author(s)

Wolfram Stacklies

nObs,pcaRes-method 37

nObs,pcaRes-method

Get the number of observations used to build the PCA model.

# Description

Get the number of observations used to build the PCA model.

# Usage

```
nObs(object, ...)
```

# Arguments

object pcaRes object ... Not used

#### Value

Number of observations

### Author(s)

Henning Redestig

 ${\sf nP,pcaRes-method}$ 

Get number of PCs

# Description

Get number of PCs

### Usage

```
nP(object, ...)
```

### **Arguments**

object pcaRes object ... not used

### Value

Number of PCs

### Author(s)

Henning Redestig

38 nVar,pcaRes-method

nPcs,pcaRes-method

Get number of PCs.

# Description

Get number of PCs.

### Usage

```
nPcs(object, ...)
```

# Arguments

object pcaRes object ... not used

#### Value

Number of PCs

#### Note

Try to use link{nP} instead since nPcs tend to clash with argument names.

## Author(s)

Henning Redestig

nVar,pcaRes-method

Get the number of variables used to build the PCA model.

# Description

Get the number of variables used to build the PCA model.

# Usage

```
nVar(object, ...)
```

# Arguments

object pcaRes object ... Not used

optiAlgCgd 39

# Value

Number of variables

# Author(s)

Henning Redestig

 ${\tt optiAlgCgd}$ 

Conjugate gradient optimization

# Description

Conjugate gradient optimization

# Usage

```
optiAlgCgd(nlnet, trainIn, trainOut, verbose = FALSE)
```

# Arguments

nlnet The nlnet

trainIn Training data

trainOut fitted data

verbose logical, print messages

# Value

•••

# Author(s)

Henning Redestig, Matthias Scholz

40 pca

orth

Calculate an orthonormal basis

# Description

ONB = orth(mat) is an orthonormal basis for the range of matrix mat. That is, ONB' \* ONB = I, the columns of ONB span the same space as the columns of mat, and the number of columns of ONB is the rank of mat.

### Usage

```
orth(mat, skipInac = FALSE)
```

#### **Arguments**

matrix to calculate orthonormal base

skipInac do not include components with precision below .Machine\$double.eps if TRUE

#### Value

orthonormal basis for the range of matrix

### Author(s)

Wolfram Stacklies

рса

Perform principal component analysis

# **Description**

Perform PCA on a numeric matrix for visualisation, information extraction and missing value imputation.

```
pca(object, method, nPcs = 2, scale = c("none", "pareto", "vector",
   "uv"), center = TRUE, completeObs = TRUE, subset = NULL,
   cv = c("none", "q2"), ...)
```

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#### **Arguments**

Numerical matrix with (or an object coercible to such) with samples in rows and variables as columns. Also takes ExpressionSet in which case the transposed expression matrix is used. Can also be a data frame in which case all numberic variables are used to fit the PCA.

method

One of the methods reported by listPcaMethods(). Can be left missing in which case the svd PCA is chosen for data without missing values and nipalsPca for data with missing values

Number of principal components to calculate.

Scaling, see prep.

scale Scaling, see prep.
center Centering, see prep.

completeObs Sets the completeObs slot on the resulting pcaRes object containing the original

data with but with all NAs replaced with the estimates.

subset A subset of variables to use for calculating the model. Can be column names or

indices.

cv character naming a the type of cross-validation to be performed.

... Arguments to prep, the chosen pca method and Q2.

#### **Details**

This method is wrapper function for the following set of pca methods:

**svd:** Uses classical prcomp. See documentation for svdPca.

**nipals:** An iterative method capable of handling small amounts of missing values. See documentation for nipalsPca.

**rnipals:** Same as nipals but implemented in R.

**bpca:** An iterative method using a Bayesian model to handle missing values. See documentation for bpca.

**ppca:** An iterative method using a probabilistic model to handle missing values. See documentation for ppca.

svdImpute: Uses expectation maximation to perform SVD PCA on incomplete data. See documentation for svdImpute.

Scaling and centering is part of the PCA model and handled by prep.

#### Value

A pcaRes object.

#### Author(s)

Wolfram Stacklies, Henning Redestig

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#### References

Wold, H. (1966) Estimation of principal components and related models by iterative least squares. In Multivariate Analysis (Ed., P.R. Krishnaiah), Academic Press, NY, 391-420.

Shigeyuki Oba, Masa-aki Sato, Ichiro Takemasa, Morito Monden, Ken-ichi Matsubara and Shin Ishii. A Bayesian missing value estimation method for gene expression profile data. *Bioinformatics*, 19(16):2088-2096, Nov 2003.

Troyanskaya O. and Cantor M. and Sherlock G. and Brown P. and Hastie T. and Tibshirani R. and Botstein D. and Altman RB. - Missing value estimation methods for DNA microarrays. *Bioinformatics*. 2001 Jun;17(6):520-5.

#### See Also

prcomp, princomp, nipalsPca, svdPca

#### **Examples**

```
data(iris)
## Usually some kind of scaling is appropriate
pcIr <- pca(iris, method="svd", nPcs=2)</pre>
pcIr <- pca(iris, method="nipals", nPcs=3, cv="q2")</pre>
## Get a short summary on the calculated model
summary(pcIr)
plot(pcIr)
## Scores and loadings plot
slplot(pcIr, sl=as.character(iris[,5]))
## use an expressionset and ggplot
data(sample.ExpressionSet)
pc <- pca(sample.ExpressionSet)</pre>
df <- merge(scores(pc), pData(sample.ExpressionSet), by=0)</pre>
library(ggplot2)
ggplot(df, aes(PC1, PC2, shape=sex, color=type)) +
  geom_point() +
  xlab(paste("PC1", pc@R2[1] * 100, "% of the variance")) +
  ylab(paste("PC2", pc@R2[2] * 100, "% of the variance"))
```

pcaMethods

pcaMethods

#### **Description**

Principal Component Analysis in R

#### **Details**

Package: pcaMethods
Type: Package
Developed since: 2006
License: GPL (>=3)
LazyLoad: yes

Provides Bayesian PCA, Probabilistic PCA, Nipals PCA, Inverse Non-Linear PCA and the conventional SVD PCA. A cluster based method for missing value estimation is included for comparison. BPCA, PPCA and NipalsPCA may be used to perform PCA on incomplete data as well as for accurate missing value estimation. A set of methods for printing and plotting the results is also provided. All PCA methods make use of the same data structure (pcaRes) to provide a unique interface to the PCA results. Developed at the Max-Planck Institute for Molecular Plant Physiology, Golm, Germany, RIKEN Plant Science Center Yokohama, Japan, and CAS-MPG Partner Institute for Computational Biology (PICB) Shanghai, P.R. China

#### Author(s)

Wolfram Stacklies, Henning Redestig

pcaMethods-deprecated Deprecated methods for pcaMethods

#### **Description**

**plotR2** Lack of relevance for this plot and the fact that it can not show cross-validation based diagnostics in the same plot makes it redundant with the introduction of a dedicated plot function for pcaRes. The new plot only shows R2cum but the result is pretty much the same.

### Author(s)

Henning Redestig

pcaNet

Class representation of the NLPCA neural net

### Description

This is a class representation of a non-linear PCA neural network. The nlpcaNet class is not meant for user-level usage.

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#### **Details**

Creating Objects

new("nlpcaNet", net=[the network structure], hierarchic=[hierarchic design], fct=[the functions at each layer], fkt=[the functions used for forward propagation], weightDecay=[incremental decrease of weight changes over iterations (between 0 and 1)], featureSorting=[sort features or not], dataDist=[represents the present values], inverse=[net is inverse mode or not], fCount=[amount of times features were sorted], componentLayer=[which layer is the 'bottleneck' (principal components)],erro=[the used error function], gradient=[the used gradient method], weights=[the present weights], maxIter=[the amount of iterations that was done], scalingFactor=[the scale of the original matrix])

Slots

**net** "matrix", matrix showing the representation of the neural network, e.g. (2,4,6) for a network with two features, a hidden layer and six output neurons (original variables).

**hierarchic** "list", the hierarchic design of the network, holds 'idx' (), 'var' () and layer (which layer is the principal component layer).

fct "character", a vector naming the functions that will be applied on each layer. "linr" is linear (i.e.) standard matrix products and "tanh" means that the arcus tangens is applied on the result of the matrix product (for non-linearity).

**fkt** "character", same as fct but the functions used during back propagation.

weightDecay "numeric", the value that is used to incrementally decrease the weight changes to ensure convergence.

**featureSorting** "logical", indicates if features will be sorted or not. This is used to make the NLPCA assume properties closer to those of standard PCA were the first component is more important for reconstructing the data than the second component.

dataDist "matrix", a matrix of ones and zeroes indicating which values will add to the errror.

**inverse** "logical", network is inverse mode (currently only inverse is supported) or not. Eg. the case when we have truly missing values and wish to impute them.

**fCount** "integer", Counter for the amount of times features were really sorted.

**componentLayer** "numeric", the index of 'net' that is the component layer.

error "function", the used error function. Currently only one is provided errorHierarchic.

gradient "function", the used gradient function. Currently only one is provided derrorHierarchic

weights "list", A list holding managements of the weights. The list has two functions, weights\$current() and weights\$set() which access a matrix in the local environment of this object.

maxIter "integer", the amount of iterations used to train this network.

**scalingFactor** "numeric", training the network is best made with 'small' values so the original data is scaled down to a suitable range by division with this number.

Methods

vector2matrices Returns the weights in a matrix representation.

### Author(s)

Henning Redestig

pcaRes 45

#### See Also

nlpca

pcaRes

Class for representing a PCA result

#### **Description**

This is a class representation of a PCA result

#### **Details**

### **Creating Objects**

new("pcaRes", scores=[the scores], loadings=[the loadings], nPcs=[amount of PCs], R2cum=[cumulative
R2], nObs=[amount of observations], nVar=[amount of variables], R2=[R2 for each individual
PC], sDev=[stdev for each individual PC], centered=[was data centered], center=[original
means], varLimit=[what variance limit was exceeded], method=[method used to calculate
PCA], missing=[amount of NAs], completeObs=[estimated complete observations])

#### Slots

scores "matrix", the calculated scores loadings "matrix", the calculated loadings **R2cum** "numeric", the cumulative R2 values **sDev** "numeric", the individual standard deviations of the score vectors R2 "numeric", the individual R2 values cvstat "numeric", cross-validation statistics nObs "numeric", number of observations nVar "numeric", number of variables centered "logical", data was centered or not center "numeric", the original variable centers scaled "logical", data was scaled or not scl "numeric", the original variable scales varLimit "numeric", the exceeded variance limit **nPcs,nP** "numeric", the number of calculated PCs method "character", the method used to perform PCA missing "numeric", the total amount of missing values in original data completeObs "matrix", the estimated complete observations network "nlpcaNet", the network used by non-linear PCA

Methods (not necessarily exhaustive)

46 plot.pcaRes

```
print Print function
```

summary Extract information about PC relevance

screeplot Plot a barplot of standard deviations for PCs

slplot Make a side by side score and loadings plot

nPcs Get the number of PCs

**nObs** Get the number of observations

cvstat Cross-validation statistics

nVar Get the number of variables

loadings Get the loadings

scores Get the scores

**dim** Get the dimensions (number of observations, number of features)

centered Get a logical indicating if centering was done as part of the model

center Get the averages of the original variables.

completeObs Get the imputed data set

method Get a string naming the used PCA method

**sDev** Get the standard deviations of the PCs

scaled Get a logical indicating if scaling was done as part of the model

scl Get the scales of the original variablesb

**R2cum** Get the cumulative R2

#### Author(s)

Henning Redestig

plot.pcaRes

Plot diagnostics (screeplot)

### Description

Plot the computed diagnostics of PCA model to get an idea of their importance. Note though that the standard screeplot shows the standard deviations for the PCs this method shows the R2 values which empirically shows the importance of the P's and is thus applicable for any PCA method rather than just SVD based PCA.

```
## S3 method for class 'pcaRes'
plot(x, y = NULL, main = deparse(substitute(object)),
  col = gray(c(0.9, 0.5)), ...)
```

plotPcs 47

# **Arguments**

| X    | pcaRes The pcaRes object.    |
|------|------------------------------|
| у    | not used                     |
| main | title of the plot            |
| col  | Colors of the bars           |
|      | further arguments to barplot |

#### **Details**

If cross-validation was done for the PCA the plot will also show the CV based statistics. A common rule-of-thumb for determining the optimal number of PCs is the PC where the CV diagnostic is at its maximum but not very far from  $\mathbb{R}^2$ .

#### Value

None, used for side effect.

#### Author(s)

Henning Redestig

### See Also

screeplot

### **Examples**

```
data(metaboliteData)
pc <- pca(t(metaboliteData), nPcs=5, cv="q2", scale="uv")
plot(pc)</pre>
```

plotPcs

Plot many side by side scores XOR loadings plots

### **Description**

A function that can be used to visualise many PCs plotted against each other

```
plotPcs(object, pcs = 1:nP(object), type = c("scores", "loadings"),
    sl = NULL, hotelling = 0.95, ...)
```

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### **Arguments**

| object    | pcaRes a pcaRes object   |
|-----------|--|
| pcs       | numeric which pcs to plot  |
| type      | character Either "scores" or "loadings" for scores or loadings plot respectively             |
| sl        | character Text labels to plot instead of a point, if NULL points are plotted instead of text |
| hotelling | numeric Significance level for the confidence ellipse. NULL means that no ellipse is drawn.  |
|           | Further arguments to pairs on which this function is based.                                  |

#### **Details**

Uses pairs to provide side-by-side plots. Note that this function only plots scores or loadings but not both in the same plot.

### Value

None, used for side effect.

### Author(s)

Henning Redestig

### See Also

```
prcomp, pca, princomp, slplot
```

# **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4], nPcs=3, method="svd")
plotPcs(pcIr, col=as.integer(iris[,4]) + 1)</pre>
```

ppca

Probabilistic PCA

### **Description**

Implementation of probabilistic PCA (PPCA). PPCA allows to perform PCA on incomplete data and may be used for missing value estimation. This script was implemented after the Matlab version provided by Jakob Verbeek ( see <a href="http://lear.inrialpes.fr/~verbeek/">http://lear.inrialpes.fr/~verbeek/</a>) and the draft "EM Algorithms for PCA and Sensible PCA" written by Sam Roweis.

```
ppca(Matrix, nPcs = 2, seed = NA, threshold = 1e-05,
  maxIterations = 1000, ...)
```

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### Arguments

Matrix — Data containing the variables in columns and observations in rows.

The data may contain missing values, denoted as NA.

nPcs numeric – Number of components to estimate. The preciseness of the missing

value estimation depends on the number of components, which should resemble

the internal structure of the data.

seed numeric Set the seed for the random number generator. PPCA creates fills the

initial loading matrix with random numbers chosen from a normal distribution. Thus results may vary slightly. Set the seed for exact reproduction of your re-

sults.

threshold Convergence threshold.

maxIterations the maximum number of allowed iterations

... Reserved for future use. Currently no further parameters are used.

#### **Details**

Probabilistic PCA combines an EM approach for PCA with a probabilistic model. The EM approach is based on the assumption that the latent variables as well as the noise are normal distributed.

In standard PCA data which is far from the training set but close to the principal subspace may have the same reconstruction error. PPCA defines a likelihood function such that the likelihood for data far from the training set is much lower, even if they are close to the principal subspace. This allows to improve the estimation accuracy.

A method called kEstimate is provided to estimate the optimal number of components via cross validation. In general few components are sufficient for reasonable estimation accuracy. See also the package documentation for further discussion on what kind of data PCA-based missing value estimation is advisable.

### Complexity:

Runtime is linear in the number of data, number of data dimensions and number of principal components.

**Convergence:** The threshold indicating convergence was changed from 1e-3 in 1.2.x to 1e-5 in the current version leading to more stable results. For reproducability you can set the seed (parameter seed) of the random number generator. If used for missing value estimation, results may be checked by simply running the algorithm several times with changing seed, if the estimated values show little variance the algorithm converged well.

### Value

Standard PCA result object used by all PCA-based methods of this package. Contains scores, loadings, data mean and more. See pcaRes for details.

### Note

Requires MASS. It is not recommended to use this function directly but rather to use the pca() wrapper function.

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#### Author(s)

Wolfram Stacklies

#### See Also

```
bpca, svdImpute, prcomp, nipalsPca, pca, pcaRes.
```

### **Examples**

```
## Load a sample metabolite dataset with 5\% missing values (metaboliteData)
data(metaboliteData)
## Perform probabilistic PCA using the 3 largest components
result <- pca(t(metaboliteData), method="ppca", nPcs=3, seed=123)
## Get the estimated complete observations
cObs <- completeObs(result)
## Plot the scores
plotPcs(result, type = "scores")</pre>
```

predict-methods

Predict values from PCA.

### **Description**

Predict data using PCA model

#### Usage

```
## S3 method for class 'pcaRes'
predict(object, newdata, pcs = nP(object), pre = TRUE,
    post = TRUE, ...)

## S4 method for signature 'pcaRes'
predict(object, newdata, pcs = nP(object),
    pre = TRUE, post = TRUE, ...)
```

# Arguments

| object  | pcaRes the pcaRes object of interest.                                      |
|---------|--|
| newdata | matrix new data with same number of columns as the used to compute object. |
| pcs     | numeric The number of PC's to consider                                     |
| pre     | pre-process newdata based on the pre-processing chosen for the PCA model   |
| post    | unpre-process the final data (add the center back etc)                     |
|         | Not passed on anywhere, included for S3 consistency.                       |

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#### **Details**

This function extracts the predict values from a pcaRes object for the PCA methods SVD, Nipals, PPCA and BPCA. Newdata is first centered if the PCA model was and then scores (T) and data (X) is 'predicted' according to:  $\hat{T} = X_{new}P$   $\hat{X}_{new} = \hat{T}P'$ . Missing values are set to zero before matrix multiplication to achieve NIPALS like treatment of missing values.

#### Value

A list with the following components:

scores The predicted scores x The predicted data

#### Author(s)

Henning Redestig

### **Examples**

```
data(iris)
hidden <- sample(nrow(iris), 50)
pcIr <- pca(iris[-hidden,1:4])
pcFull <- pca(iris[,1:4])
irisHat <- predict(pcIr, iris[hidden,1:4])
cor(irisHat$scores[,1], scores(pcFull)[hidden,1])</pre>
```

prep

Pre-process a matrix for PCA

## **Description**

Scaling and centering a matrix.

### Usage

```
prep(object, scale = c("none", "pareto", "vector", "uv"),
  center = TRUE, eps = 1e-12, simple = TRUE, reverse = FALSE, ...)
```

### **Arguments**

object

Numerical matrix (or an object coercible to such) with samples in rows and variables as columns. Also takes ExpressionSet in which case the transposed expression matrix is used.

scale

One of "UV" (unit variance  $a=a/\sigma_a$ ) "vector" (vector normalisation b=b/||b||), "pareto" (sqrt UV) or "none" to indicate which scaling should be used to scale the matrix with a variables and b samples. Can also be a vector of scales which should be used to scale the matrix. NULL value is interpreted as "none".

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| center  | Either a logical which indicates if the matrix should be mean centred or not, or a vector with averages which should be suntracted from the matrix. NULL value is interpreted as FALSE   |
|---------|--|
| eps     | Minimum variance, variable with lower variance are not scaled and warning is issued instead.   |
| simple  | Logical indicating if only the data should be returned or a list with the pre-<br>processing statistics as well.   |
| reverse | Logical indicating if matrix should be 'post-processed' instead by multiplying each column with its scale and adding the center. In this case, center and scale should be vectors with the statistics (no warning is issued if not, instead output becomes the same as input). |
| •••     | Only used for passing through arguments.   |
|         |  |

#### **Details**

Does basically the same as scale but adds some alternative scaling options and functionality for treating pre-processing as part of a model.

#### Value

A pre-processed matrix or a list with

center a vector with the estimated centers scale a vector with the estimated scales data the pre (or post) processed data

### Author(s)

Henning Redestig

# **Examples**

```
object <- matrix(rnorm(50), nrow=10)
res <- prep(object, scale="uv", center=TRUE, simple=FALSE)
obj <- prep(object, scale=res$scale, center=res$center)
## same as original
sum((object - prep(obj, scale=res$scale, center=res$center, rev=TRUE))^2)</pre>
```

Q2 Cross-validation for PCA

# **Description**

Internal cross-validation can be used for estimating the level of structure in a data set and to optimise the choice of number of principal components.

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#### Usage

```
Q2(object, originalData = completeObs(object), fold = 5, nruncv = 1,
  type = c("krzanowski", "impute"), verbose = interactive(),
  variables = 1:nVar(object), ...)
```

#### **Arguments**

object A pcaRes object (result from previous PCA analysis.)

originalData The matrix (or ExpressionSet) that used to obtain the pcaRes object.

fold The number of groups to divide the data in.

nruncv The number of times to repeat the whole cross-validation

type krzanowski or imputation type cross-validation

verbose boolean If TRUE Q2 outputs a primitive progress bar.

variables indices of the variables to use during cross-validation calculation. Other vari-

ables are kept as they are and do not contribute to the total sum-of-squares.

... Further arguments passed to the pca function called within Q2.

#### **Details**

This method calculates  $Q^2$  for a PCA model. This is the cross-validated version of  $R^2$  and can be interpreted as the ratio of variance that can be predicted independently by the PCA model. Poor (low)  $Q^2$  indicates that the PCA model only describes noise and that the model is unrelated to the true data structure. The definition of  $Q^2$  is:

$$Q^{2} = 1 - \frac{\sum_{i}^{k} \sum_{j}^{n} (x - \hat{x})^{2}}{\sum_{i}^{k} \sum_{j}^{n} x^{2}}$$

for the matrix x which has n rows and k columns. For a given number of PC's x is estimated as  $\hat{x} = TP'$  (T are scores and P are loadings). Although this defines the leave-one-out cross-validation this is not what is performed if fold is less than the number of rows and/or columns. In 'impute' type CV, diagonal rows of elements in the matrix are deleted and the re-estimated. In 'krzanowski' type CV, rows are sequentially left out to build fold PCA models which give the loadings. Then, columns are sequentially left out to build fold models for scores. By combining scores and loadings from different models, we can estimate completely left out values. The two types may seem similar but can give very different results, krzanowski typically yields more stable and reliable result for estimating data structure whereas impute is better for evaluating missing value imputation performance. Note that since Krzanowski CV operates on a reduced matrix, it is not possible estimate Q2 for all components and the result vector may therefore be shorter than nPcs(object).

#### Value

A matrix or vector with  $Q^2$  estimates.

### Author(s)

Henning Redestig, Ondrej Mikula

#### References

Krzanowski, WJ. Cross-validation in principal component analysis. Biometrics. 1987(43):3,575-584

### **Examples**

```
data(iris)
x <- iris[,1:4]
pcIr <- pca(x, nPcs=3)
q2 <- Q2(pcIr, x)
barplot(q2, main="Krzanowski CV", xlab="Number of PCs", ylab=expression(Q^2))
## q2 for a single variable
Q2(pcIr, x, variables=2)
pcIr <- pca(x, nPcs=3, method="nipals")
q2 <- Q2(pcIr, x, type="impute")
barplot(q2, main="Imputation CV", xlab="Number of PCs", ylab=expression(Q^2))</pre>
```

R2cum, pcaRes-method

Cumulative R2 is the total ratio of variance that is being explained by the model

# Description

Cumulative R2 is the total ratio of variance that is being explained by the model

### Usage

```
## S4 method for signature 'pcaRes'
R2cum(object, ...)
```

#### **Arguments**

object a pcaRes model ... Not used

### Value

Get the cumulative R2

### Author(s)

Henning Redestig

R2VX,pcaRes-method 55

R2VX, pcaRes-method R2 goodness of fit

### **Description**

Flexible calculation of R2 goodness of fit.

### Usage

```
## S4 method for signature 'pcaRes'
R2VX(object, direction = c("variables",
   "observations", "complete"), data = completeObs(object),
   pcs = nP(object))
```

# Arguments

object a PCA model object

direction choose between calculating R2 per variable, per observation or for the entire

data with 'variables', 'observations' or 'complete'.

data the data used to fit the model

pcs the number of PCs to use to calculate R2

#### Value

A vector with R2 values

#### Author(s)

Henning Redestig

# **Examples**

```
R2VX(pca(iris))
```

rediduals-methods Residuals values from a PCA model.

# Description

This function extracts the residuals values from a pcaRes object for the PCA methods SVD, Nipals, PPCA and BPCA

repmat repmat

### Usage

```
## S3 method for class 'pcaRes'
residuals(object, data = completeObs(object), ...)
## S4 method for signature 'pcaRes'
residuals(object, data = completeObs(object), ...)
## S4 method for signature 'pcaRes'
resid(object, data = completeObs(object), ...)
```

#### **Arguments**

object pcaRes the pcaRes object of interest.

data matrix The data that was used to calculate the PCA model (or a different dataset

to e.g. adress its proximity to the model).

... Passed on to predict.pcaRes. E.g. setting the number of used components.

#### Value

A matrix with the residuals

#### Author(s)

Henning Redestig

### **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4])
head(residuals(pcIr, iris[,1:4]))</pre>
```

repmat

Replicate and tile an array.

# Description

Creates a large matrix B consisting of an M-by-N tiling of copies of A

### Usage

```
repmat(mat, M, N)
```

## Arguments

mat numeric matrix

M number of copies in vertical directionN number of copies in horizontal direction

RnipalsPca 57

### Value

Matrix consiting of M-by-N tiling copies of input matrix

### Author(s)

Wolfram Stacklies

| RnipalsPca | NIPALS PCA implemented in R |  |
|------------|-----------------------------|--|
|------------|-----------------------------|--|

### **Description**

PCA by non-linear iterative partial least squares

### Usage

```
RnipalsPca(Matrix, nPcs = 2, varLimit = 1, maxSteps = 5000,
    threshold = 1e-06, verbose = interactive(), ...)
```

# Arguments

| Matrix    | Pre-processed (centered, scaled) numerical matrix samples in rows and variables as columns.  |
|-----------|--|
| nPcs      | Number of components that should be extracted.   |
| varLimit  | Optionally the ratio of variance that should be explained. nPcs is ignored if $varLimit < 1$   |
| maxSteps  | Defines how many iterations can be done before algorithm should abort (happens almost exclusively when there were some wrong in the input data).     |
| threshold | The limit condition for judging if the algorithm has converged or not, specifically if a new iteration is done if $(T_{old}-T)^T(T_{old}-T)>1$ imit. |
| verbose   | Show simple progress information.  |
| • • •     | Only used for passing through arguments.   |

### **Details**

Can be used for computing PCA on a numeric matrix using either the NIPALS algorithm which is an iterative approach for estimating the principal components extracting them one at a time. NIPALS can handle a small amount of missing values. It is not recommended to use this function directly but rather to use the pca() wrapper function. There is a C++ implementation given as nipalsPca which is faster.

### Value

A pcaRes object.

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#### Author(s)

Henning Redestig

#### References

Wold, H. (1966) Estimation of principal components and related models by iterative least squares. In Multivariate Analysis (Ed., P.R. Krishnaiah), Academic Press, NY, 391-420.

#### See Also

```
prcomp, princomp, pca
```

### **Examples**

```
data(metaboliteData)
mat <- prep(t(metaboliteData))
## c++ version is faster
system.time(pc <- RnipalsPca(mat, method="rnipals", nPcs=2))
system.time(pc <- nipalsPca(mat, nPcs=2))
## better use pca()
pc <- pca(t(metaboliteData), method="rnipals", nPcs=2)</pre>
```

robustPca

PCA implementation based on robustSvd

# **Description**

This is a PCA implementation robust to outliers in a data set. It can also handle missing values, it is however NOT intended to be used for missing value estimation. As it is based on robustSVD we will get an accurate estimation for the loadings also for incomplete data or for data with outliers. The returned scores are, however, affected by the outliers as they are calculated inputData X loadings. This also implies that you should look at the returned R2/R2cum values with caution. If the data show missing values, scores are caluclated by just setting all NA - values to zero. This is not expected to produce accurate results. Please have also a look at the manual page for robustSvd. Thus this method should mainly be seen as an attempt to integrate robustSvd() into the framework of this package. Use one of the other methods coming with this package (like PPCA or BPCA) if you want to do missing value estimation. It is not recommended to use this function directely but rather to use the pca() wrapper function.

```
robustPca(Matrix, nPcs = 2, verbose = interactive(), ...)
```

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#### **Arguments**

Matrix — Data containing the variables in columns and observations in rows.

The data may contain missing values, denoted as NA.

nPcs — numeric — Number of components to estimate. The preciseness of the missing value estimation depends on the number of components, which should resemble the internal structure of the data.

verbose boolean Print some output to the command line if TRUE

Reserved for future use. Currently no further parameters are used

#### **Details**

The method is very similar to the standard prcomp() function. The main difference is that robustSvd() is used instead of the conventional svd() method.

#### Value

Standard PCA result object used by all PCA-based methods of this package. Contains scores, loadings, data mean and more. See pcaRes for details. are used.

### Author(s)

Wolfram Stacklies

#### See Also

```
robustSvd, svd, prcomp,pcaRes.
```

#### **Examples**

```
## Load a complete sample metabolite data set and mean center the data
data(metaboliteDataComplete)
mdc <- scale(metaboliteDataComplete, center=TRUE, scale=FALSE)</pre>
## Now create 5\% of outliers.
      <- runif(length(mdc)) < 0.05;</pre>
mdcOut <- mdc
mdcOut[cond] <- 10</pre>
## Now we do a conventional PCA and robustPca on the original and the data
## with outliers.
## We use center=FALSE here because the large artificial outliers would
## affect the means and not allow to objectively compare the results.
          <- pca(mdc, method="svd", nPcs=10, center=FALSE)
resSvdOut <- pca(mdcOut, method="svd", nPcs=10, center=FALSE)
resRobPca <- pca(mdcOut, method="robustPca", nPcs=10, center=FALSE)
## Now we plot the results for the original data against those with outliers
## We can see that robustPca is hardly effected by the outliers.
plot(loadings(resSvd)[,1], loadings(resSvdOut)[,1])
plot(loadings(resSvd)[,1], loadings(resRobPca)[,1])
```

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robustSvd

Alternating L1 Singular Value Decomposition

#### **Description**

A robust approximation to the singular value decomposition of a rectangular matrix is computed using an alternating L1 norm (instead of the more usual least squares L2 norm). As the SVD is a least-squares procedure, it is highly susceptible to outliers and in the extreme case, an individual cell (if sufficiently outlying) can draw even the leading principal component toward itself.

#### Usage

robustSvd(x)

#### **Arguments**

Х

A matrix whose SVD decomposition is to be computed. Missing values are allowed.

#### **Details**

See Hawkins et al (2001) for details on the robust SVD algorithm. Briefly, the idea is to sequentially estimate the left and right eigenvectors using an L1 (absolute value) norm minimization.

Note that the robust SVD is able to accommodate missing values in the matrix x, unlike the usual svd function.

Also note that the eigenvectors returned by the robust SVD algorithm are NOT (in general) orthogonal and the eigenvalues need not be descending in order.

### Value

The robust SVD of the matrix is x=u d v'.

d A vector containing the singular values of x.

u A matrix whose columns are the left singular vectors of x.

v A matrix whose columns are the right singular vectors of x.

#### Note

Two differences from the usual SVD may be noted. One relates to orthogonality. In the conventional SVD, all the eigenvectors are orthogonal even if not explicitly imposed. Those returned by the AL1 algorithm (used here) are (in general) not orthogonal. Another difference is that, in the L2 analysis of the conventional SVD, the successive eigen triples (eigenvalue, left eigenvector, right eigenvector) are found in descending order of eigenvalue. This is not necessarily the case with the AL1 algorithm. Hawkins et al (2001) note that a larger eigen value may follow a smaller one.

# Author(s)

Kevin Wright, modifications by Wolfram Stacklies

scaled,pcaRes-method 61

#### References

Hawkins, Douglas M, Li Liu, and S Stanley Young (2001) Robust Singular Value Decomposition, National Institute of Statistical Sciences, Technical Report Number 122. http://www.niss.org/technicalreports/tr122.pdf

#### See Also

svd, nipals for an alternating L2 norm method that also accommodates missing data.

### **Examples**

```
## Load a complete sample metabolite data set and mean center the data
data(metaboliteDataComplete)
mdc <- prep(metaboliteDataComplete, center=TRUE, scale="none")</pre>
## Now create 5% of outliers.
cond <- runif(length(mdc)) < 0.05;</pre>
mdcOut <- mdc
mdcOut[cond] <- 10</pre>
## Now we do a conventional SVD and a robustSvd on both, the original and the
## data with outliers.
resSvd <- svd(mdc)</pre>
resSvdOut <- svd(mdcOut)</pre>
resRobSvd <- robustSvd(mdc)</pre>
resRobSvdOut <- robustSvd(mdcOut)</pre>
## Now we plot the results for the original data against those with outliers
## We can see that robustSvd is hardly affected by the outliers.
plot(resSvd$v[,1], resSvdOut$v[,1])
plot(resRobSvd$v[,1], resRobSvdOut$v[,1])
```

scaled, pcaRes-method Check if scaling was part of the PCA model

### **Description**

Check if scaling was part of the PCA model

#### Usage

```
scaled(object, ...)
```

### **Arguments**

```
object pcaRes object
... Not used
```

### Value

TRUE if scaling was part of the PCA model

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### Author(s)

Henning Redestig

scl,pcaRes-method

Get the scales (e.g. standard deviations) of the original variables

# Description

Get the scales (e.g. standard deviations) of the original variables

# Usage

```
scl(object, ...)
```

# Arguments

object pcaRes object Not used

#### Value

Vector with the scales

# Author(s)

Henning Redestig

#### See Also

prep

scores, pcaRes-method Get scores from a pcaRes object

# Description

Get scores from a pcaRes object

```
## S4 method for signature 'pcaRes'
scores(object, ...)
```

scores.pcaRes 63

# Arguments

object a pcaRes object

... not used

### Value

The scores as a matrix

# Author(s)

Henning Redestig

### See Also

scores.pcaRes

scores.pcaRes

Get scores from a pcaRes object

# Description

Get scores from a pcaRes object

# Usage

```
## S3 method for class 'pcaRes'
scores(object, ...)
```

# Arguments

object a pcaRes object

... not used

# Value

The scores as a matrix

# Author(s)

Henning Redestig

64 show-methods

sDev,pcaRes-method

*Get the standard deviations of the scores (indicates their relevance)* 

# Description

Get the standard deviations of the scores (indicates their relevance)

# Usage

```
sDev(object, ...)
```

# **Arguments**

object pcaRes object
... Not used

#### Value

Standard devations of the scores

### Author(s)

Henning Redestig

show-methods

Print/Show for pcaRes

# Description

Print basic information about pcaRes object

# Usage

```
showPcaRes(x, ...)
## S4 method for signature 'pcaRes'
print(x, ...)
## S4 method for signature 'pcaRes'
show(object)
```

#### **Arguments**

```
x a pcaRes object
```

... not used

object the object to print information about

showNniRes 65

### Value

nothing, used for its side effect

# Author(s)

Henning Redestig

showNniRes

Print a nniRes model

# Description

Print a brief description of nniRes model

# Usage

```
showNniRes(x, ...)
```

# Arguments

x An nniRes object

... Not used

#### Value

Nothing, used for side-effect

# Author(s)

Henning Redestig

simpleEllipse

Hotelling's T^2 Ellipse

# Description

Get a confidence ellipse for uncorrelated bivariate data

```
simpleEllipse(x, y, alfa = 0.95, len = 200)
```

slplot,pcaRes-method

#### **Arguments**

| X | first variable  |
|---|-----------------|
| y | second variable |

alfa confidence level of the circle
len Number of points in the circle

#### **Details**

As described in 'Introduction to multi and megavariate data analysis using PCA and PLS' by Eriksson et al. This produces very similar ellipse as compared to the ellipse function the ellipse package except that this function assumes that and y are uncorrelated (which they of are if they are scores or loadings from a PCA).

#### Value

A matrix with X and Y coordinates for the circle

### Author(s)

Henning Redestig

#### See Also

ellipse

slplot, pcaRes-method Side by side scores and loadings plot

#### **Description**

A common way of visualizing two principal components

### Usage

```
slplot(object, pcs=c(1,2), scoresLoadings=c(TRUE, TRUE),
sl="def", ll="def", hotelling=0.95, rug=TRUE, sub=NULL,...)
```

### **Arguments**

object a pcaRes object
pcs which two pcs to plot

scoresLoadings Which should be shown scores and or loadings

sl labels to plot in the scores plot labels to plot in the loadings plot

hotelling confidence interval for ellipse in the score plot

sortFeatures 67

| rug | logical, rug x axis in score plot or not  |
|-----|---|
| sub | Subtitle, defaults to annotate with amount of explained variance.   |
| ••• | Further arguments to plot functions. Prefix arguments to par() with 's' for the scores plot and 'l' for the loadings plot. I.e. cex become scex for setting character expansion in the score plot and lcex for the loadings plot. |

#### **Details**

This method is meant to be used as a quick way to visualize results, if you want a more specific plot you probably want to get the scores, loadings with scores(object), loadings(object) and then design your own plotting method.

#### Value

None, used for side effect.

#### Note

Uses layout instead of par to provide side-by-side so it works with Sweave (but can not be combined with par(mfrow=..))

# Author(s)

Henning Redestig

#### See Also

```
pca, biplot
```

# **Examples**

```
data(iris)
pcIr <- pca(iris[,1:4], scale="uv")
slplot(pcIr, sl=NULL, spch=5)
slplot(pcIr, sl=NULL, lcex=1.3, scol=as.integer(iris[,5]))</pre>
```

sortFeatures

Sort the features of NLPCA object

# Description

Sort the features of NLPCA object

```
sortFeatures(nlnet, trainIn, trainOut)
```

68 summary

# Arguments

nlnet The nlnet

trainIn Training data in

trainOut Training data after it passed through the net

# Value

..

# Author(s)

Henning Redestig

summary

Summary of PCA model

# Description

Print a brief description of the PCA model

### Usage

```
## S3 method for class 'pcaRes'
summary(object, ...)
```

# Arguments

object a pcaRes object

... Not used

### Value

Nothing, used for side-effect

# Author(s)

Henning Redestig

svdImpute 69

|--|

### **Description**

This implements the SVDimpute algorithm as proposed by Troyanskaya et al, 2001. The idea behind the algorithm is to estimate the missing values as a linear combination of the k most significant eigengenes.

### Usage

```
svdImpute(Matrix, nPcs = 2, threshold = 0.01, maxSteps = 100,
  verbose = interactive(), ...)
```

#### **Arguments**

| Matrix    | matrix – Pre-processed (centered, scaled) data with variables in columns and observations in rows. The data may contain missing values, denoted as NA.                                     |
|-----------|--|
| nPcs      | numeric – Number of components to estimate. The preciseness of the missing value estimation depends on the number of components, which should resemble the internal structure of the data. |
| threshold | The iteration stops if the change in the matrix falls below this threshold.  |
| maxSteps  | Maximum number of iteration steps.   |
| verbose   | Print some output if TRUE.   |
|           | Reserved for parameters used in future version of the algorithm  |

#### **Details**

Missing values are denoted as NA. It is not recommended to use this function directly but rather to use the pca() wrapper function.

As SVD can only be performed on complete matrices, all missing values are initially replaced by 0 (what is in fact the mean on centred data). The algorithm works iteratively until the change in the estimated solution falls below a certain threshold. Each step the eigengenes of the current estimate are calculated and used to determine a new estimate. Eigengenes denote the loadings if pca is performed considering variable (for Microarray data genes) as observations.

An optimal linear combination is found by regressing the incomplete variable against the k most significant eigengenes. If the value at position j is missing, the  $j^th$  value of the eigengenes is not used when determining the regression coefficients.

#### Value

Standard PCA result object used by all PCA-based methods of this package. Contains scores, loadings, data mean and more. See pcaRes for details.

70 svdPca

#### Note

Each iteration, standard PCA (prcomp) needs to be done for each incomplete variable to get the eigengenes. This is usually fast for small data sets, but complexity may rise if the data sets become very large.

#### Author(s)

Wolfram Stacklies

#### References

Troyanskaya O. and Cantor M. and Sherlock G. and Brown P. and Hastie T. and Tibshirani R. and Botstein D. and Altman RB. - Missing value estimation methods for DNA microarrays. *Bioinformatics*. 2001 Jun;17(6):520-5.

### **Examples**

```
## Load a sample metabolite dataset with 5\% missing values
data(metaboliteData)
## Perform svdImpute using the 3 largest components
result <- pca(metaboliteData, method="svdImpute", nPcs=3, center = TRUE)
## Get the estimated complete observations
cObs <- completeObs(result)
## Now plot the scores
plotPcs(result, type = "scores")</pre>
```

svdPca

Perform principal component analysis using singular value decomposition

#### **Description**

A wrapper function for prcomp to deliver the result as a pcaRes method. Supplied for compatibility with the rest of the pcaMethods package. It is not recommended to use this function directely but rather to use the pca() wrapper function.

### Usage

```
svdPca(Matrix, nPcs = 2, varLimit = 1, verbose = interactive(), ...)
```

# **Arguments**

| Matrix   | Pre-processed (centered and possibly scaled) numerical matrix samples in rows and variables as columns. No missing values allowed. |
|----------|--|
| nPcs     | Number of components that should be extracted.   |
| varLimit | Optionally the ratio of variance that should be explained. nPcs is ignored if $varLimit < 1$                                       |
| verbose  | Verbose complaints to matrix structure   |
|          | Only used for passing through arguments.   |

tempFixNas 71

# Value

A pcaRes object.

### Author(s)

Henning Redestig

### See Also

```
prcomp, princomp, pca
```

# **Examples**

```
data(metaboliteDataComplete)
mat <- prep(t(metaboliteDataComplete))
pc <- svdPca(mat, nPcs=2)
## better use pca()
pc <- pca(t(metaboliteDataComplete), method="svd", nPcs=2)</pre>
```

tempFixNas

Temporary fix for missing values

# Description

Simply replace completely missing rows or cols with zeroes.

#### Usage

```
tempFixNas(mat)
```

### **Arguments**

mat

a matrix

### Value

The original matrix with completely missing rows/cols filled with zeroes.

# Author(s)

Henning Redestig

vector2matrices,matrix-method

Tranform the vectors of weights to matrix structure

# Description

Tranform the vectors of weights to matrix structure

# Usage

```
## S4 method for signature 'matrix'
vector2matrices(object, net)
```

# Arguments

object an nlpcaNet

net the neural network

### Value

weights in matrix structure

### Author(s)

Henning Redestig

vector2matrices,nlpcaNet-method

Tranform the vectors of weights to matrix structure

# Description

Tranform the vectors of weights to matrix structure

# Usage

```
## S4 method for signature 'nlpcaNet'
vector2matrices(object)
```

# Arguments

object an nlpcaNet

### Value

weights in matrix structure

wasna,pcaRes-method 73

#### Author(s)

Henning Redestig

wasna,pcaRes-method

Get a matrix with indicating the elements that were missing in the input data. Convenient for estimating imputation performance.

# Description

Get a matrix with indicating the elements that were missing in the input data. Convenient for estimating imputation performance.

### Usage

```
wasna(object, ...)
```

# Arguments

object pcaRes object
... Not used

### Value

A matrix with logicals

### Author(s)

Henning Redestig

# **Examples**

```
data(metaboliteData)
data(metaboliteDataComplete)
result <- pca(metaboliteData, nPcs=2)
plot(completeObs(result)[wasna(result)], metaboliteDataComplete[wasna(result)])</pre>
```

74 weightsAccount

| weightsAccount | Create an object that holds the weights for nlpcaNet. Holds and sets weights in using an environment object. |
|----------------|--|
|                | weights at them controlled coject.   |

# Description

Create an object that holds the weights for nlpcaNet. Holds and sets weights in using an environment object.

# Usage

```
weightsAccount(w)
```

# **Arguments**

matrix – New weights

# Value

A weightsAccound with set and current functions.

# Author(s)

Henning Redestig

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